

CIFMA 2024 — 5 November 2024, Aveiro, Portugal

# *Cognitive Aspects in the Formal Modelling of Multi-party Human-computer Interactionr*

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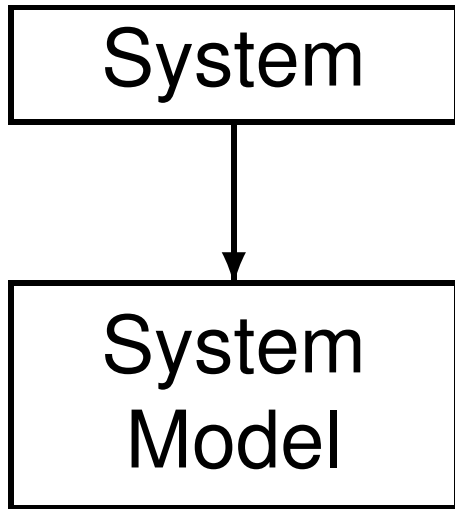
# *Background and Motivation*

- What are Formal Methods?
- Why to use Formal Methods in HCI?
- What is Multi-party HCI?

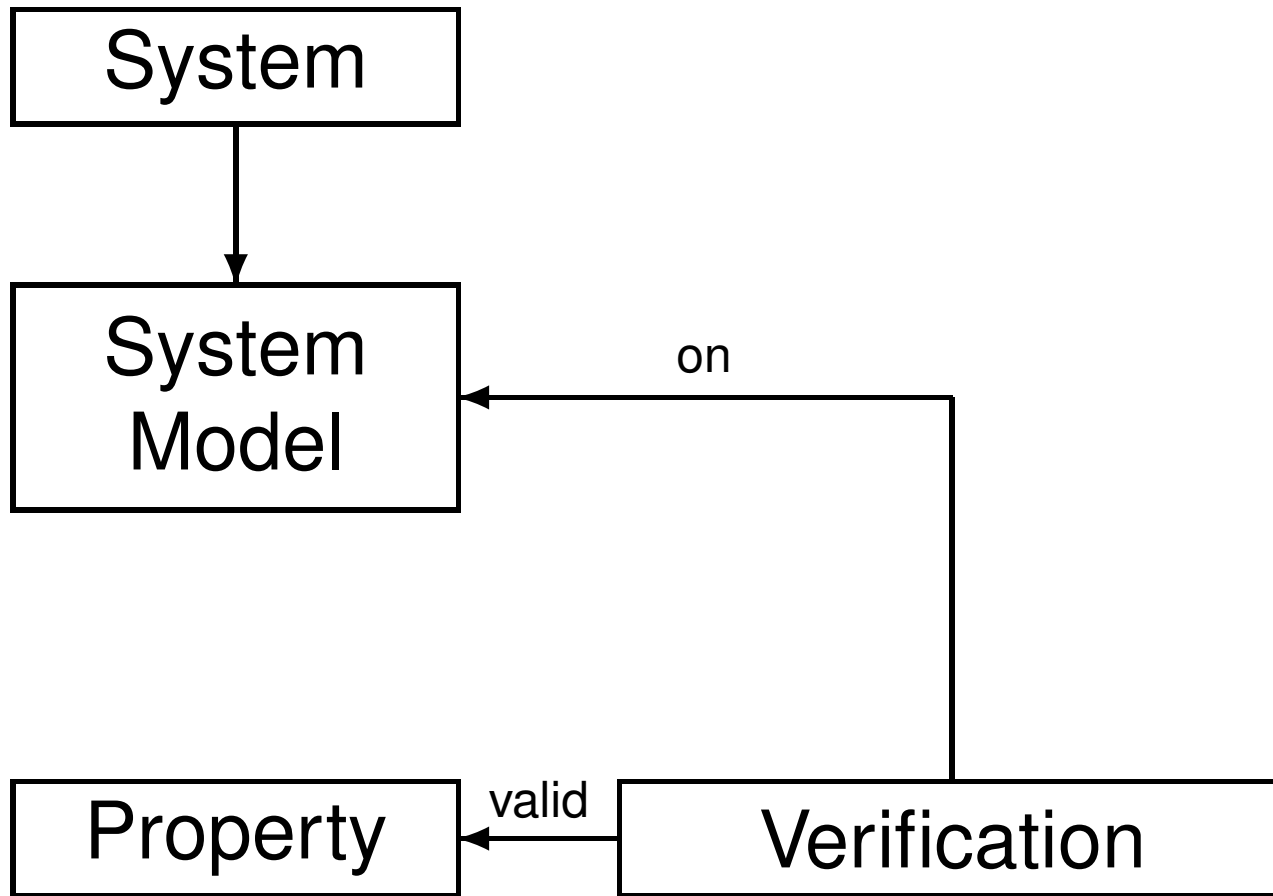
# *Formal Methods*

System

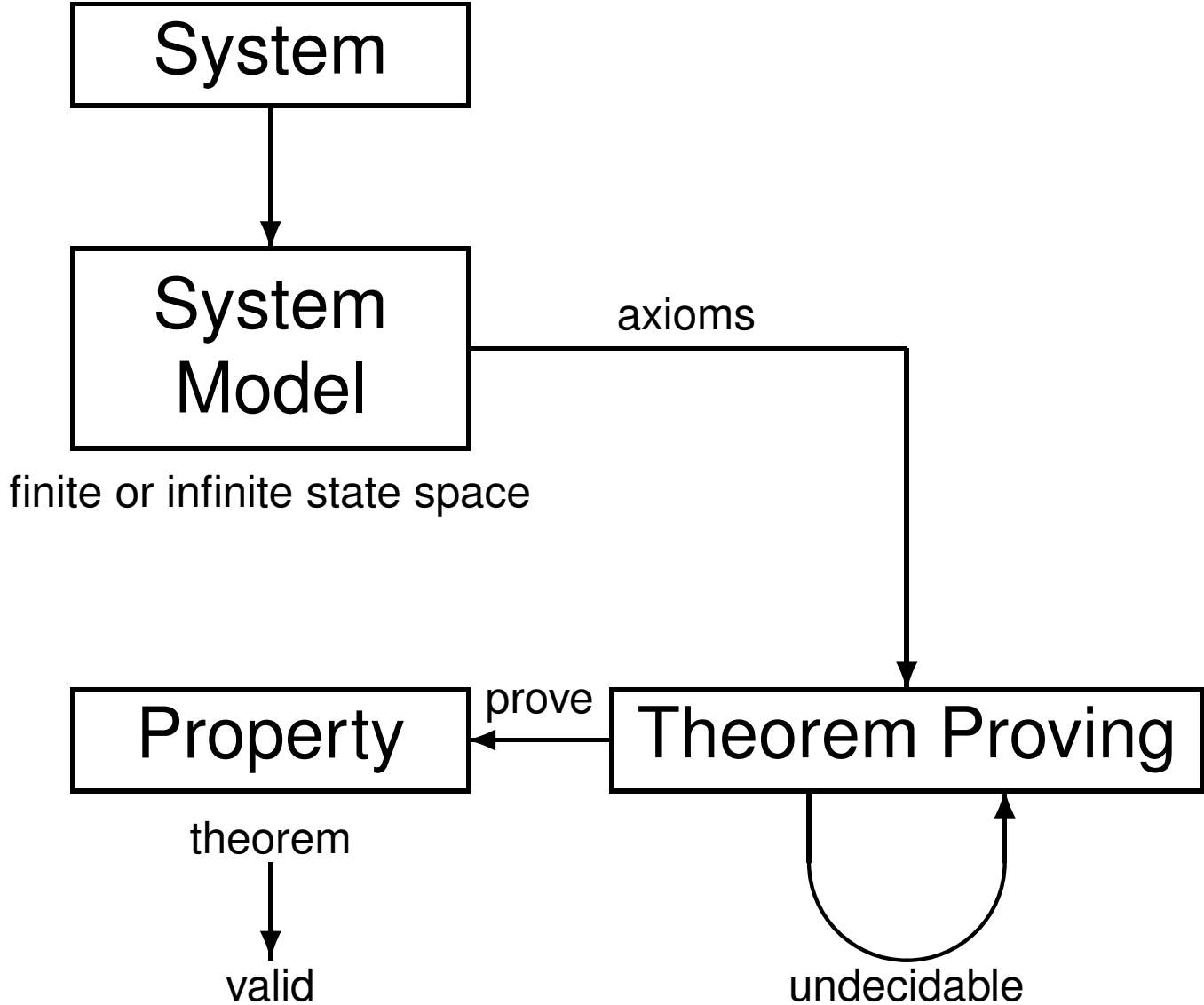
# *Formal Methods*



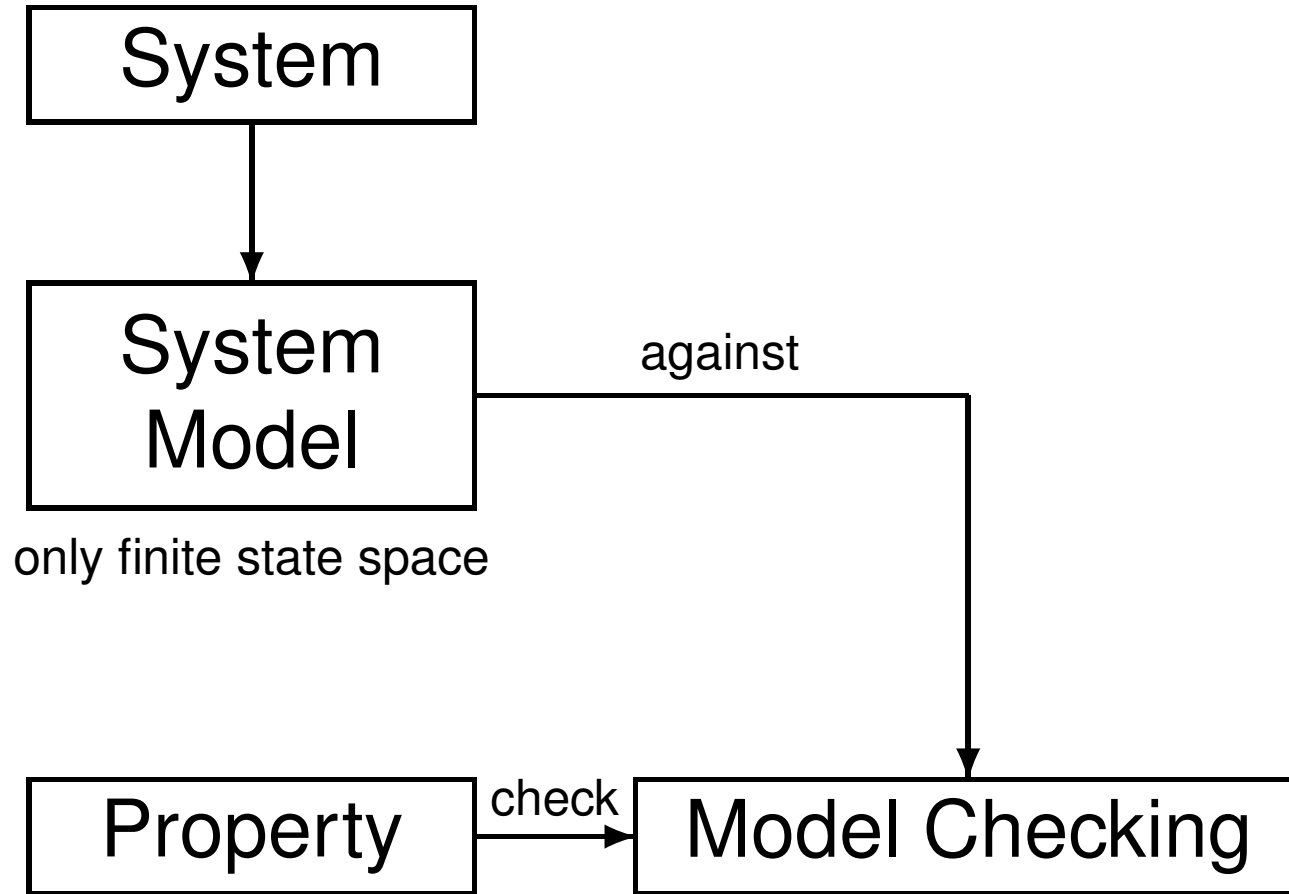
# Formal Methods



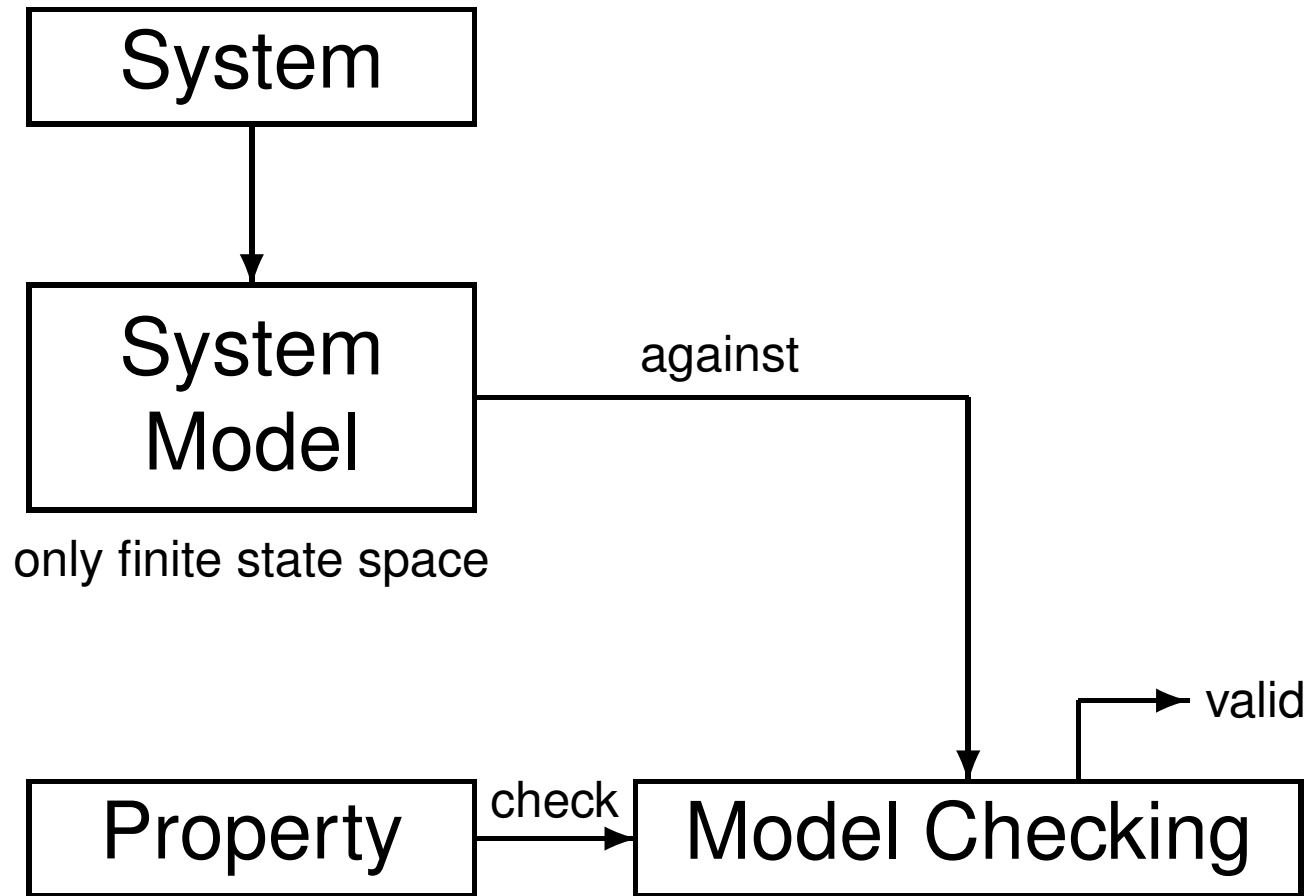
# Formal Methods



# Formal Methods

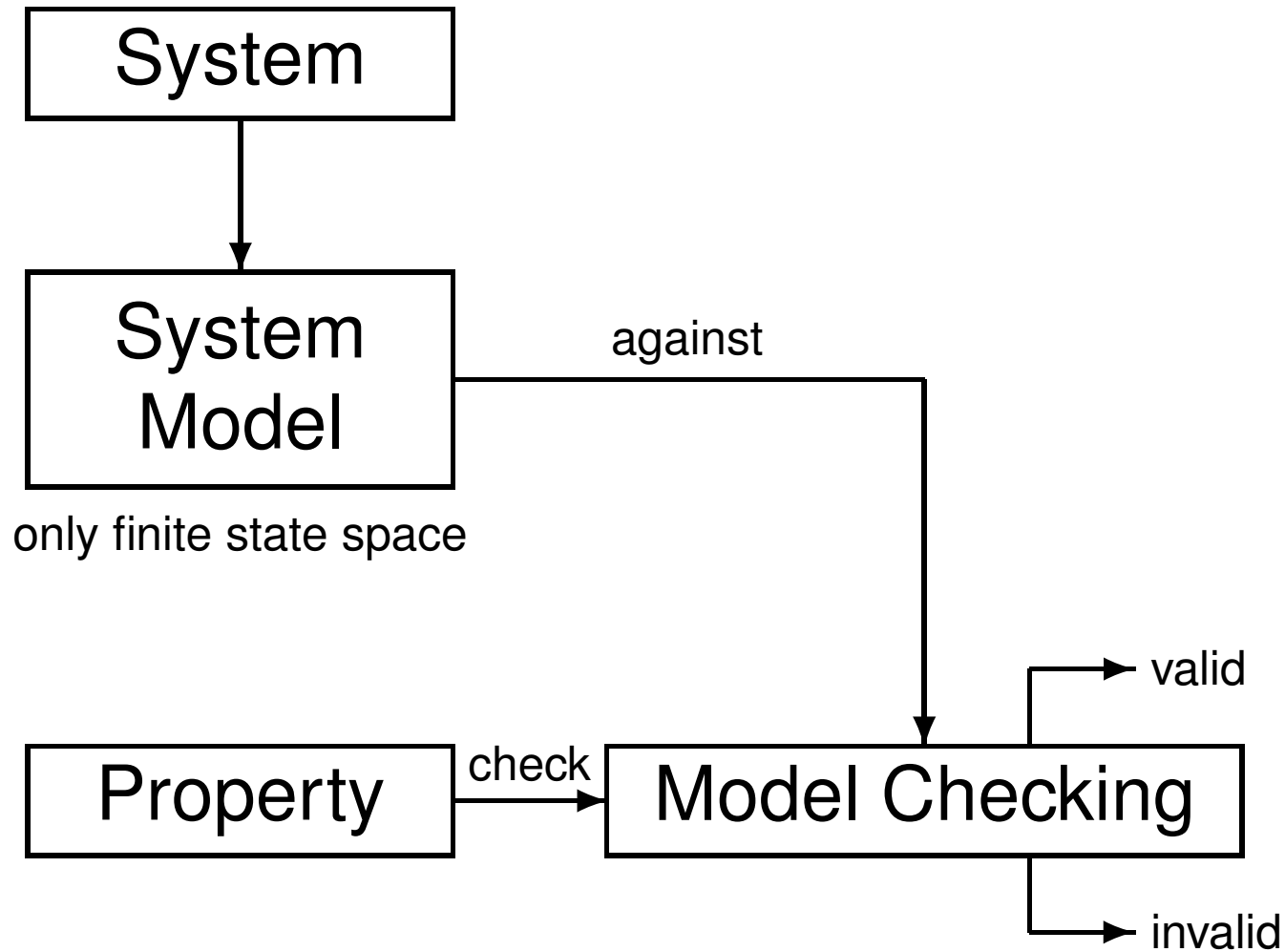


# Formal Methods

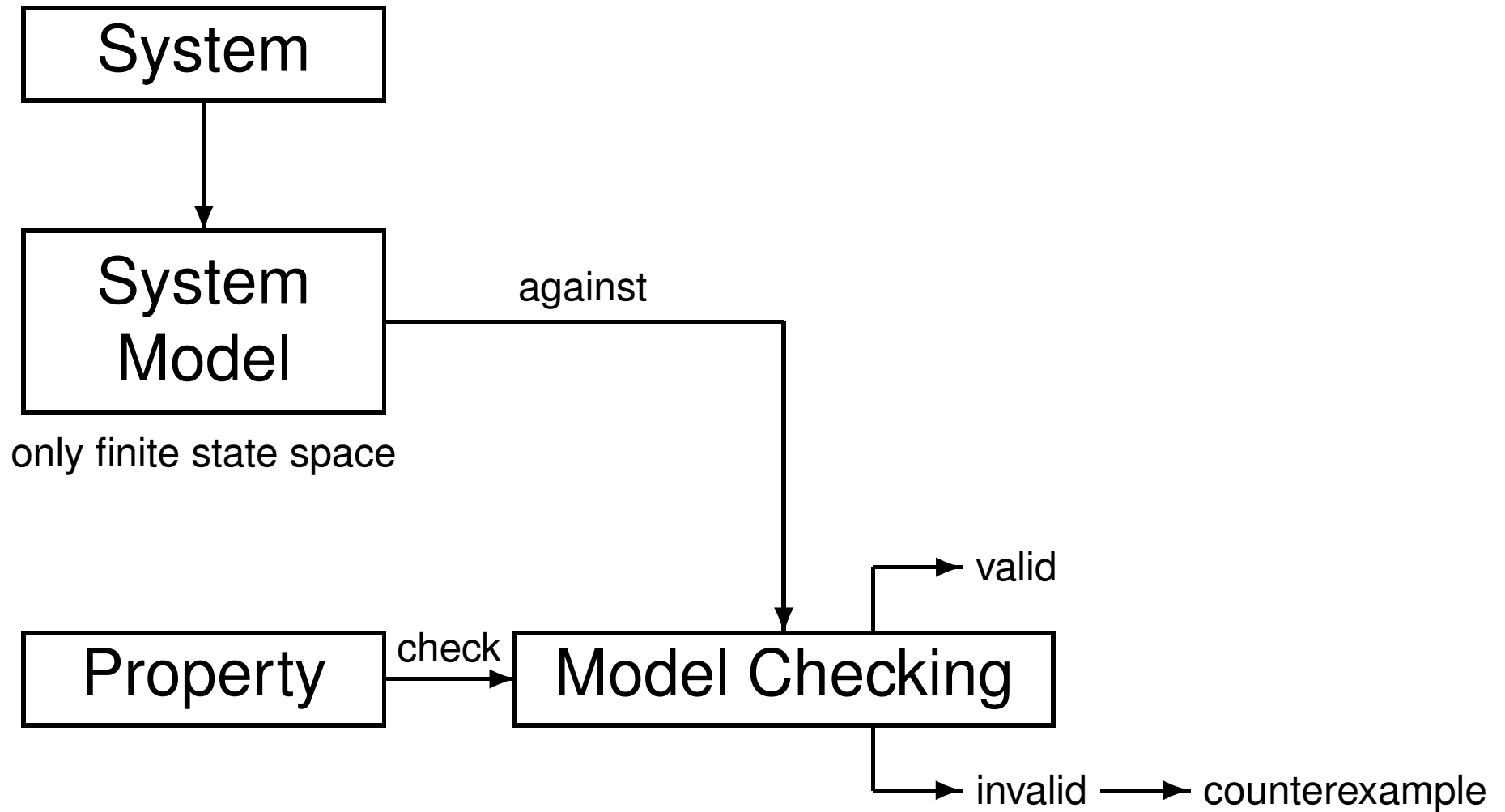




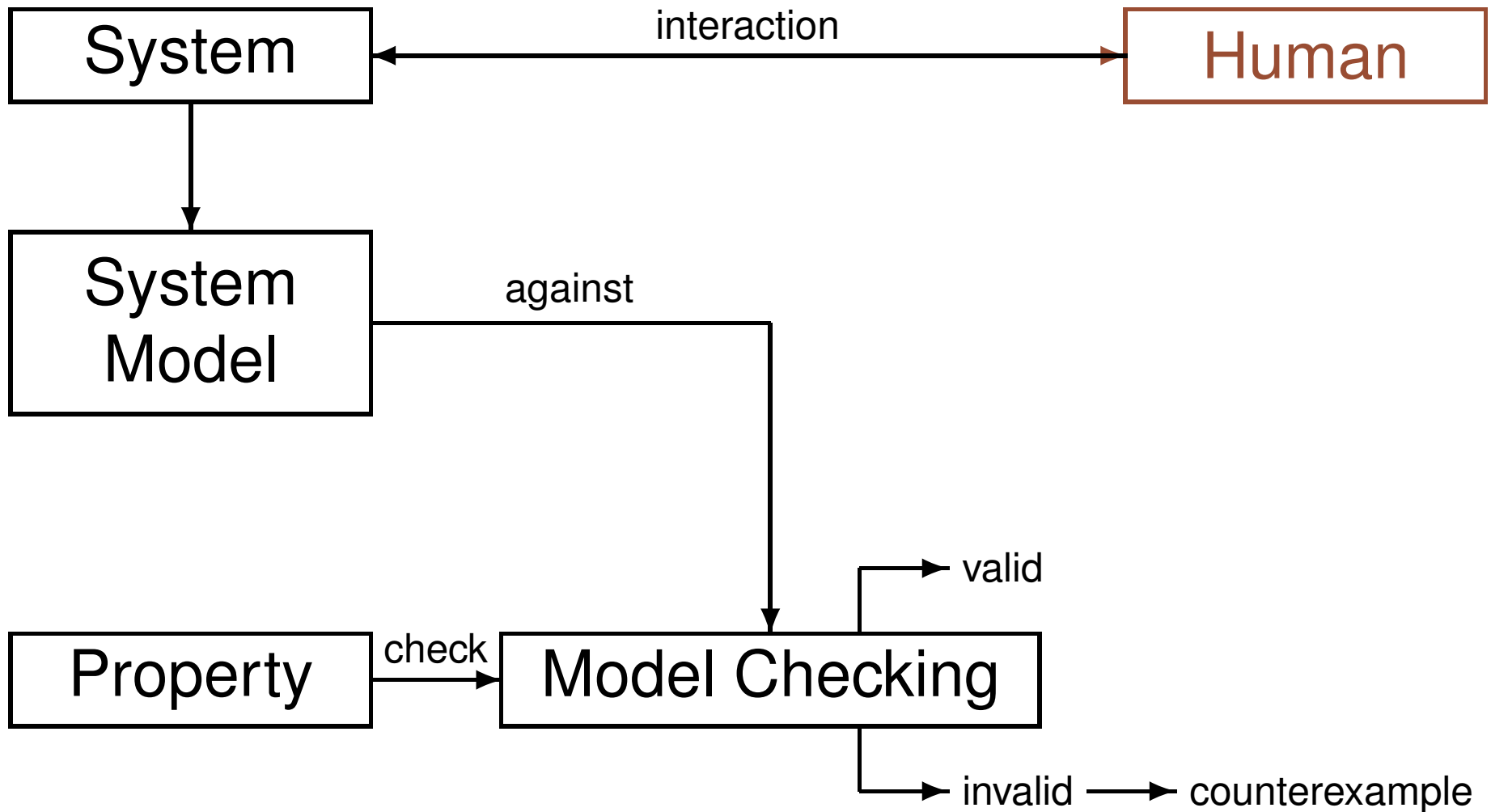
# Formal Methods



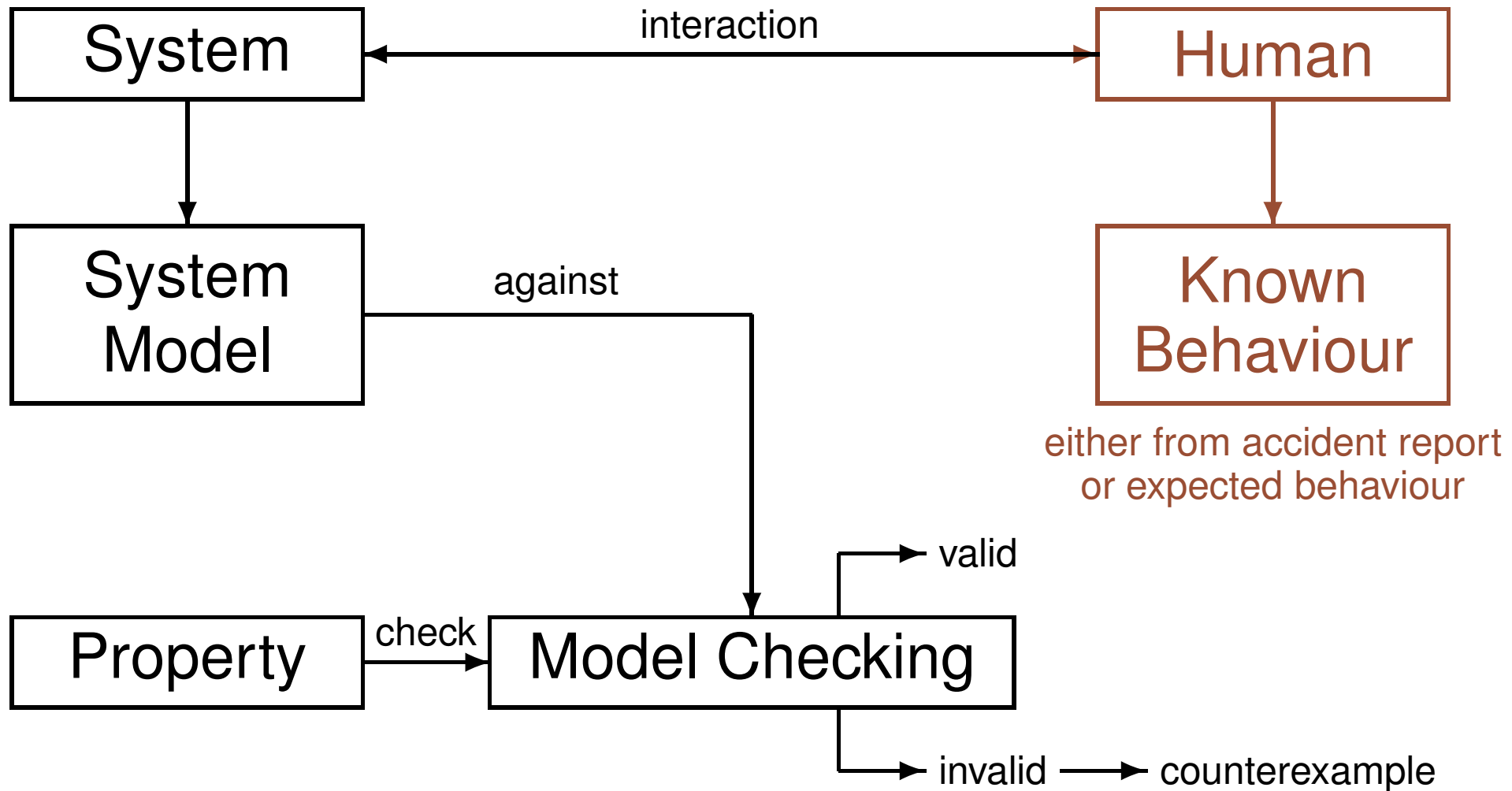
# Formal Methods



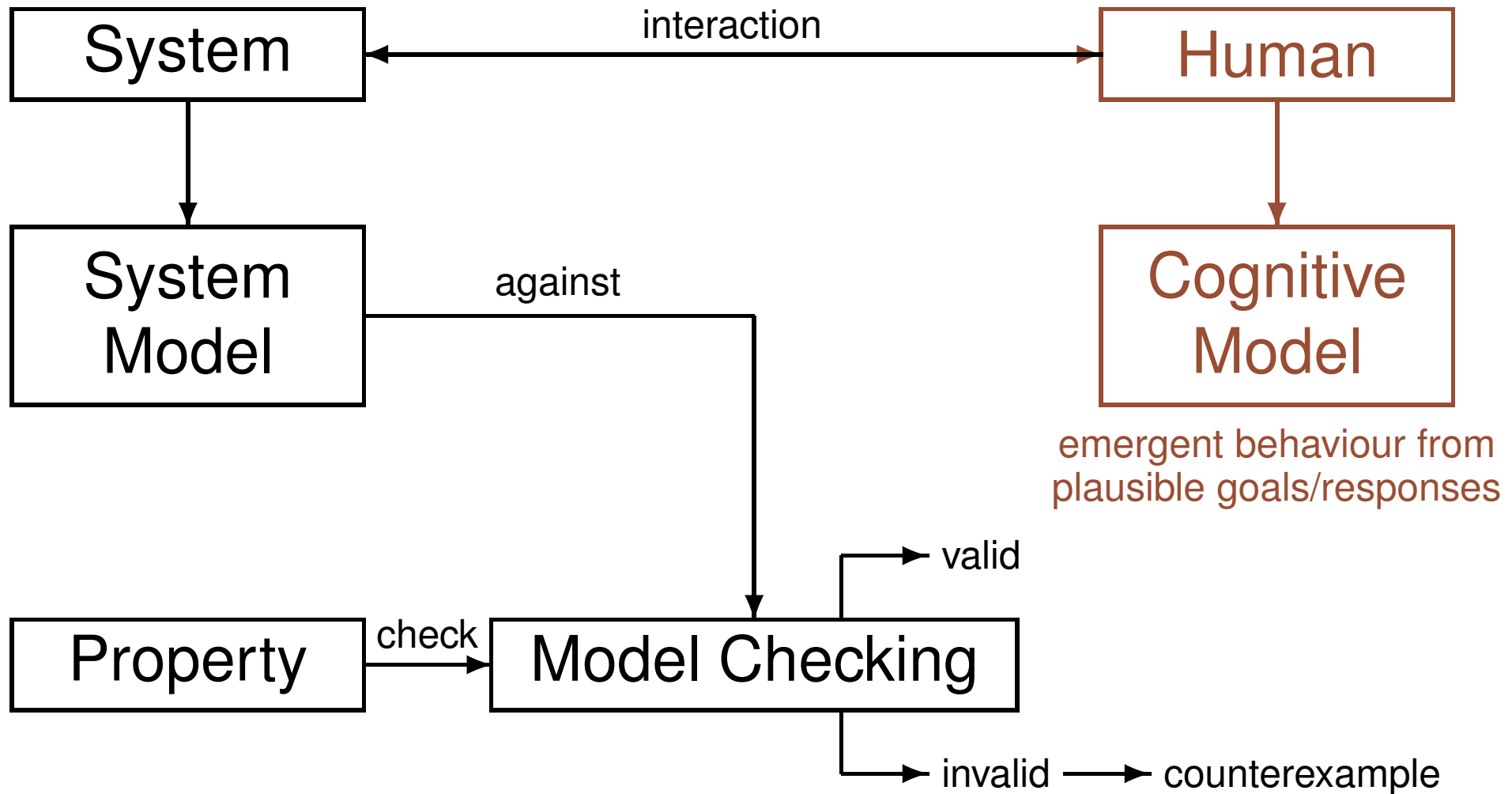
# Why to use *Formal Methods in HCI?*



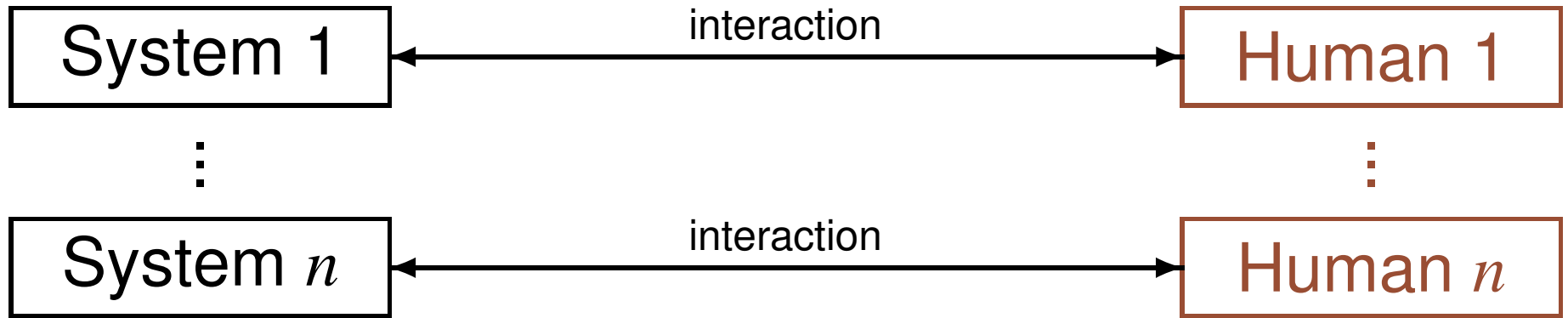
# Why to use *Formal Methods in HCI?*



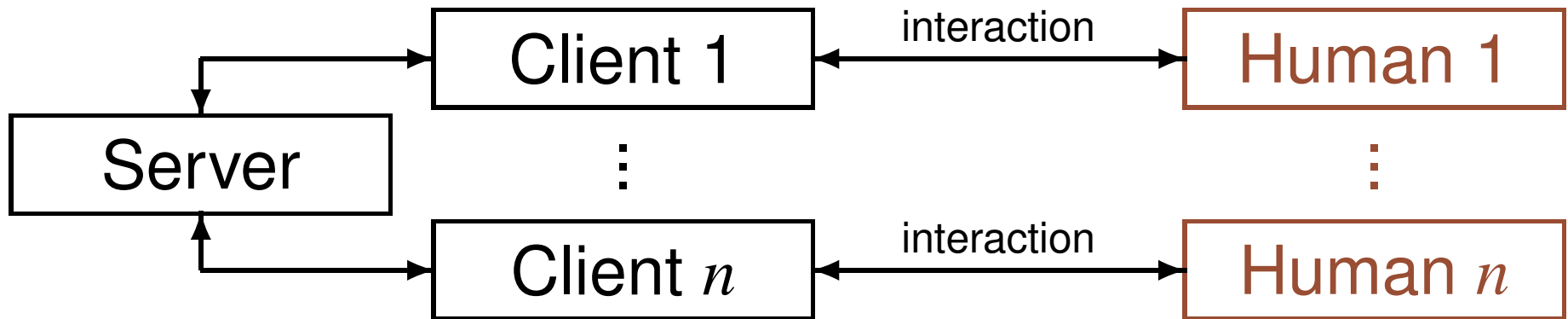
# Why to use *Formal Methods in HCI?*



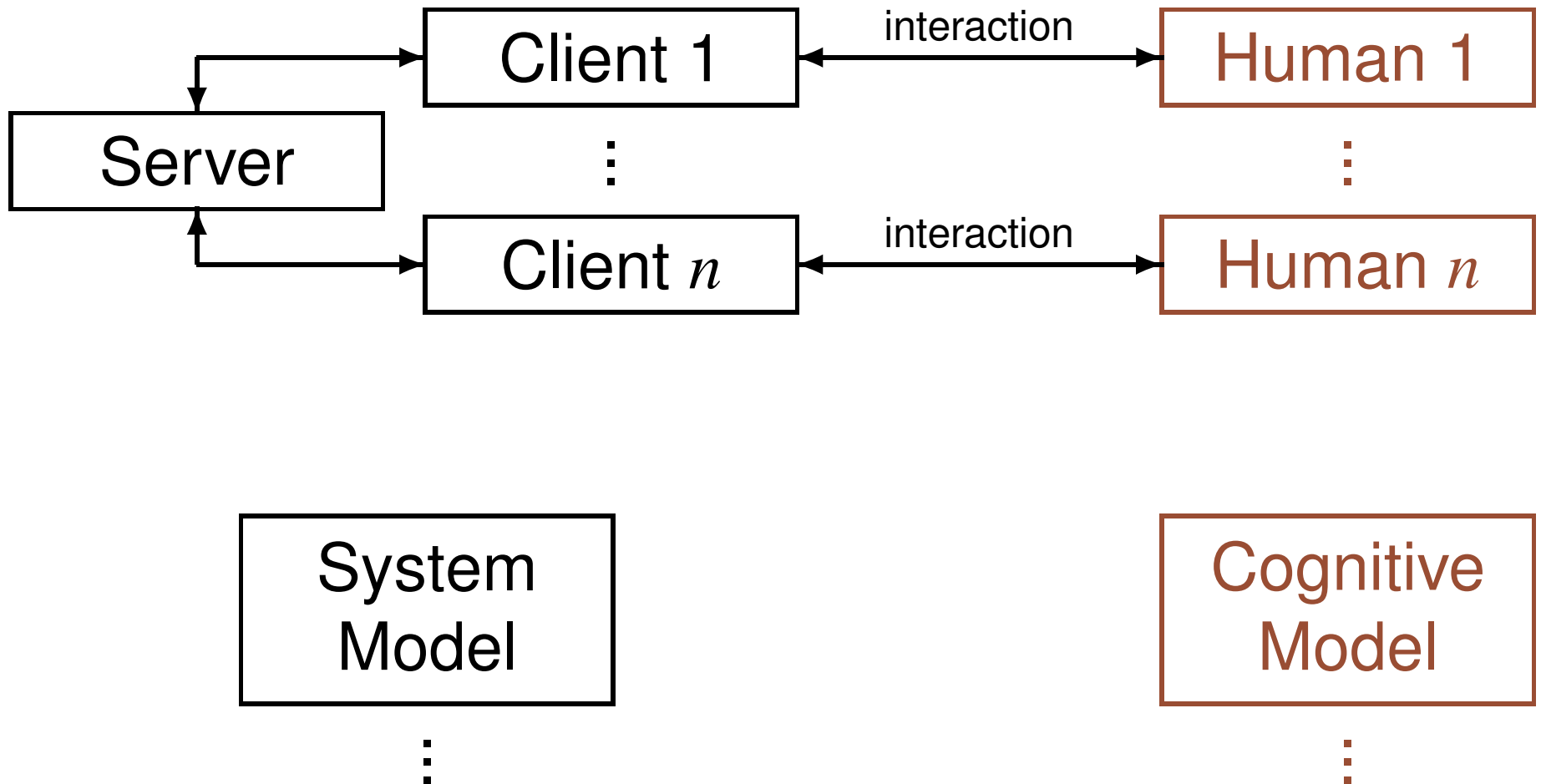
# *What is Multi-party HCI?*



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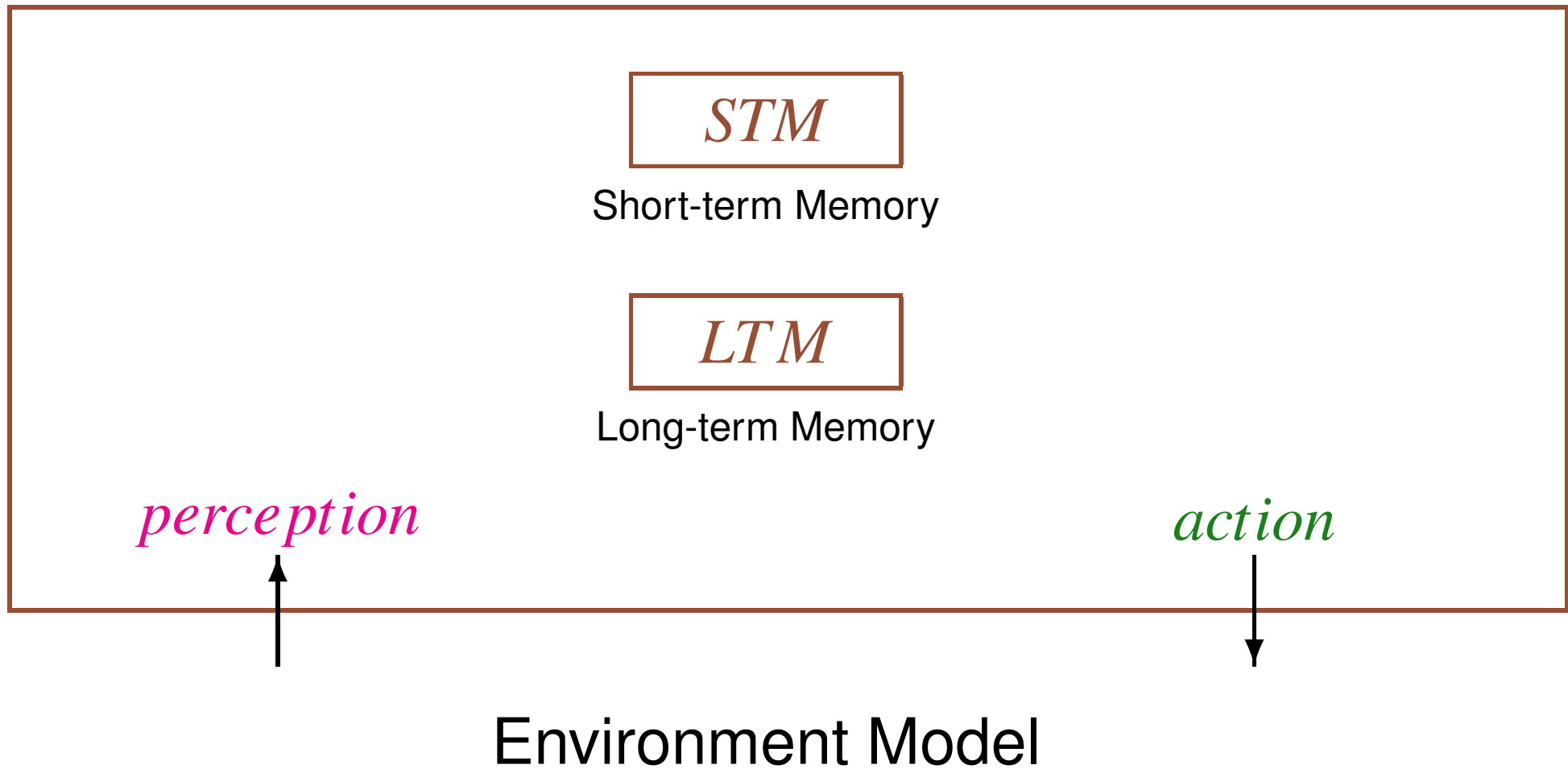


# What is Multi-party HCI?

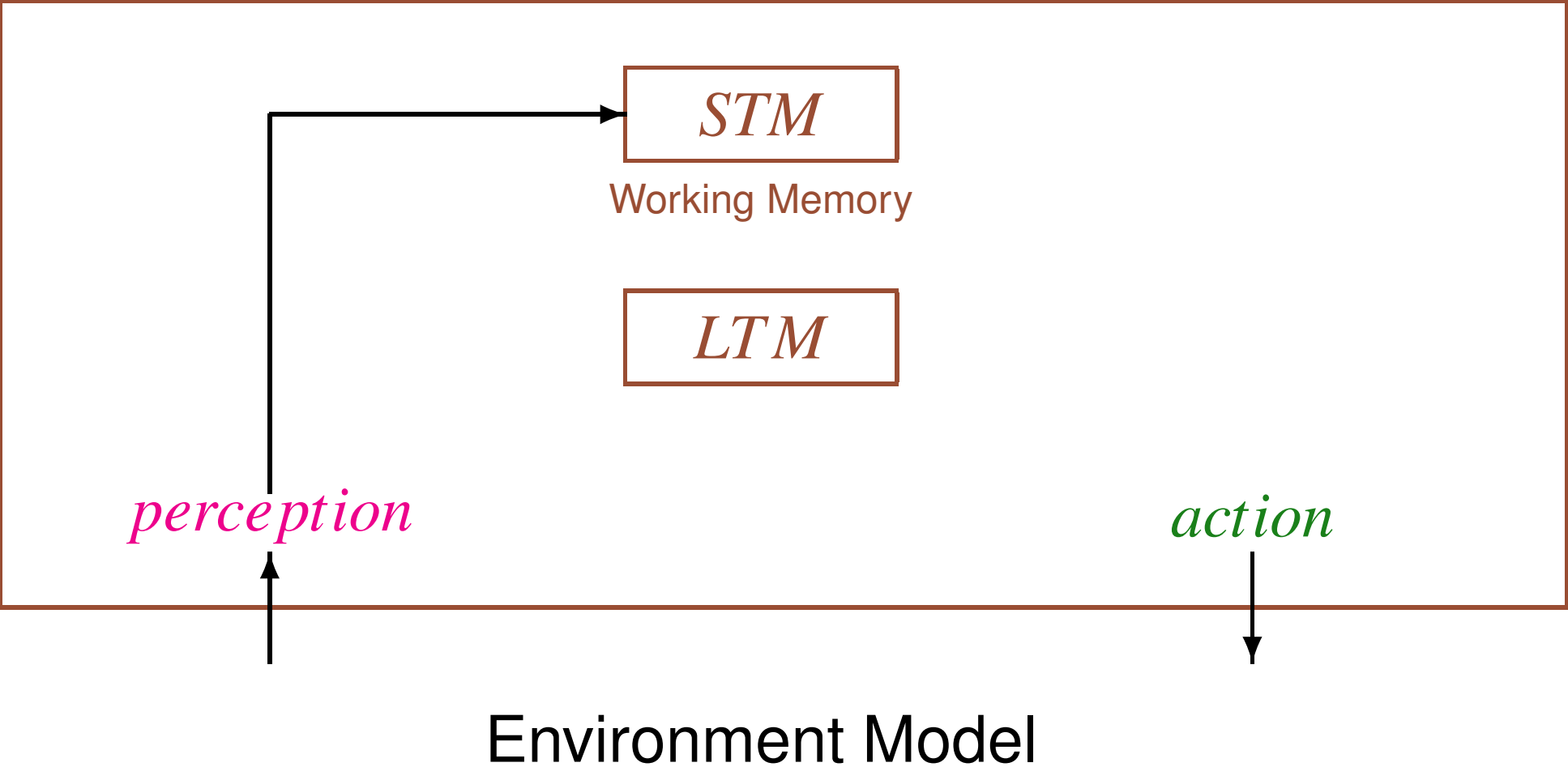




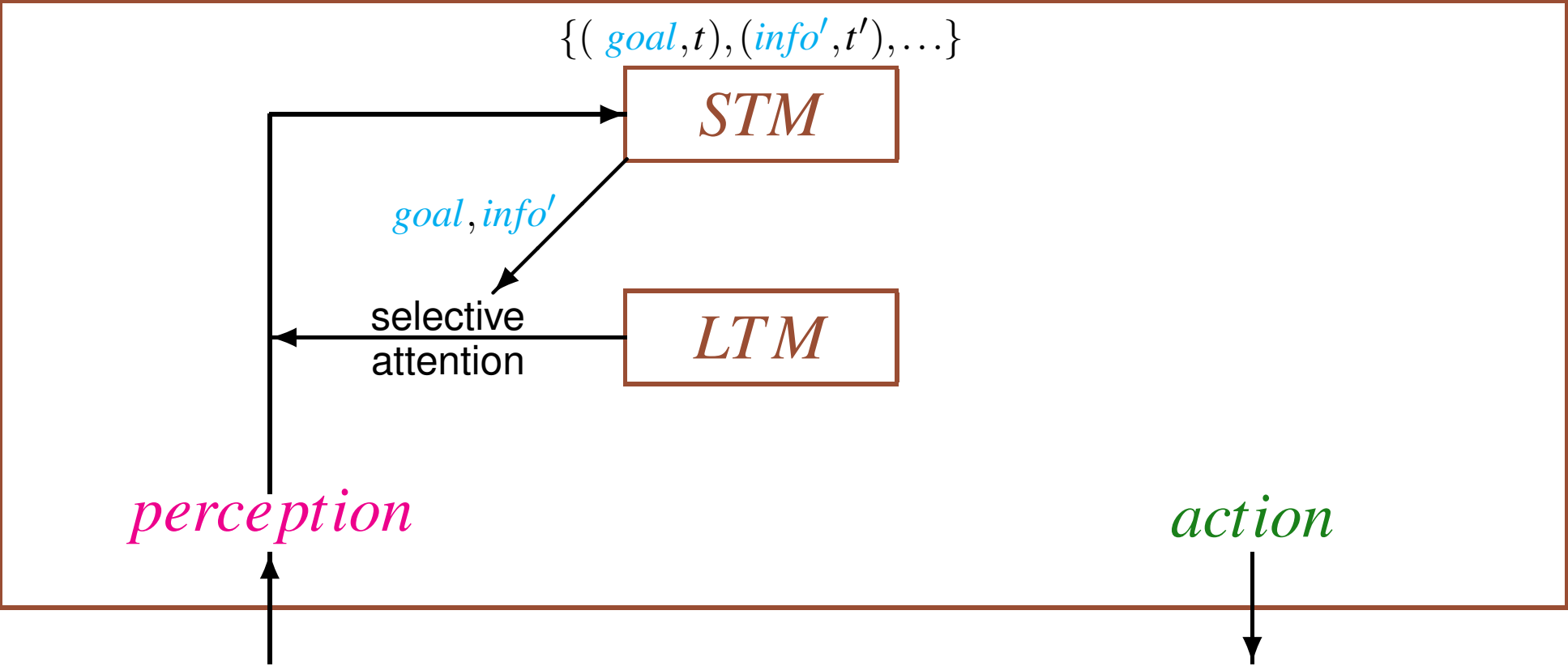
# *User Cognitive Model (UCM)*



# User Cognitive Model (UCM)

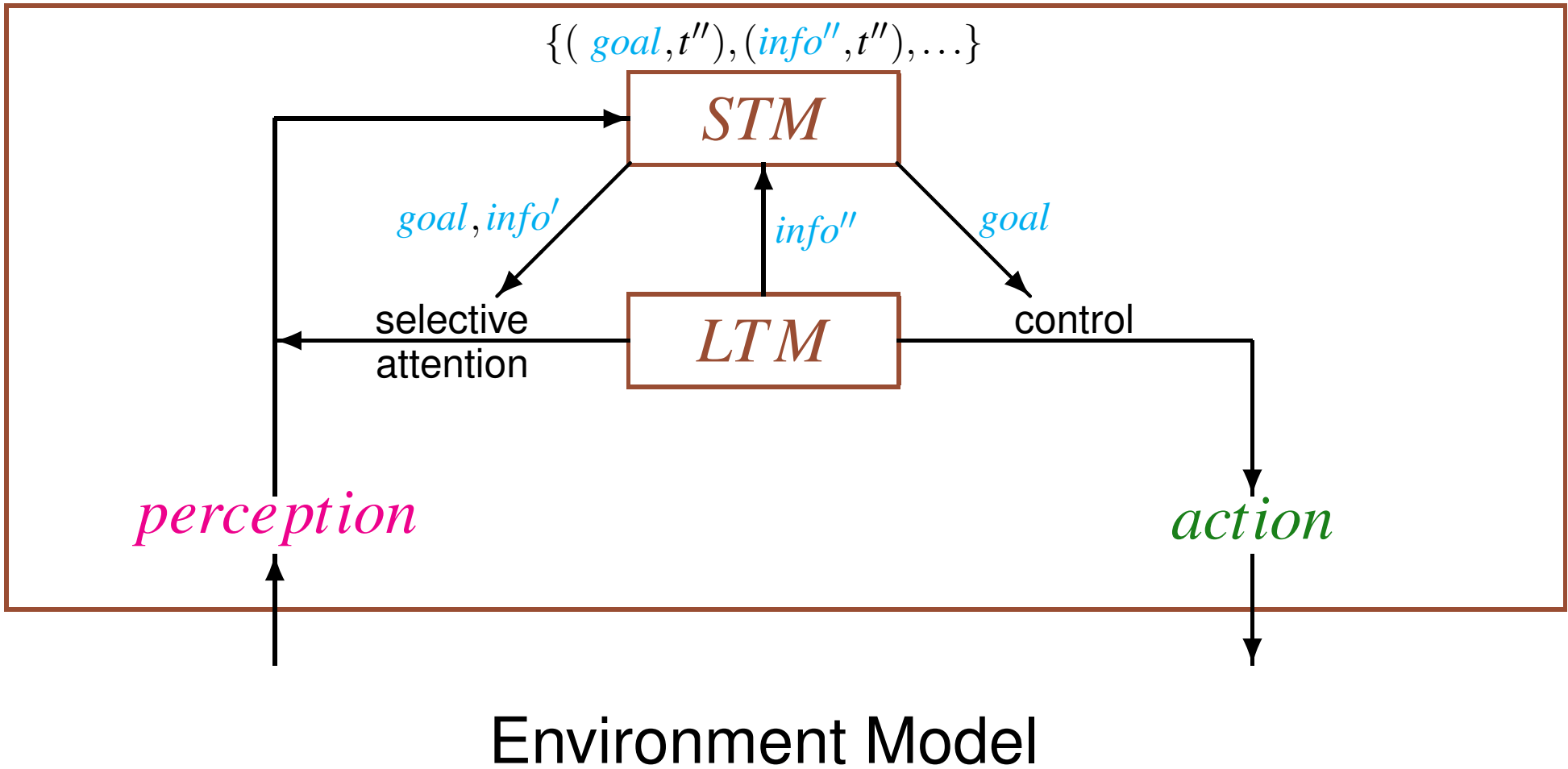


# User Cognitive Model (UCM)

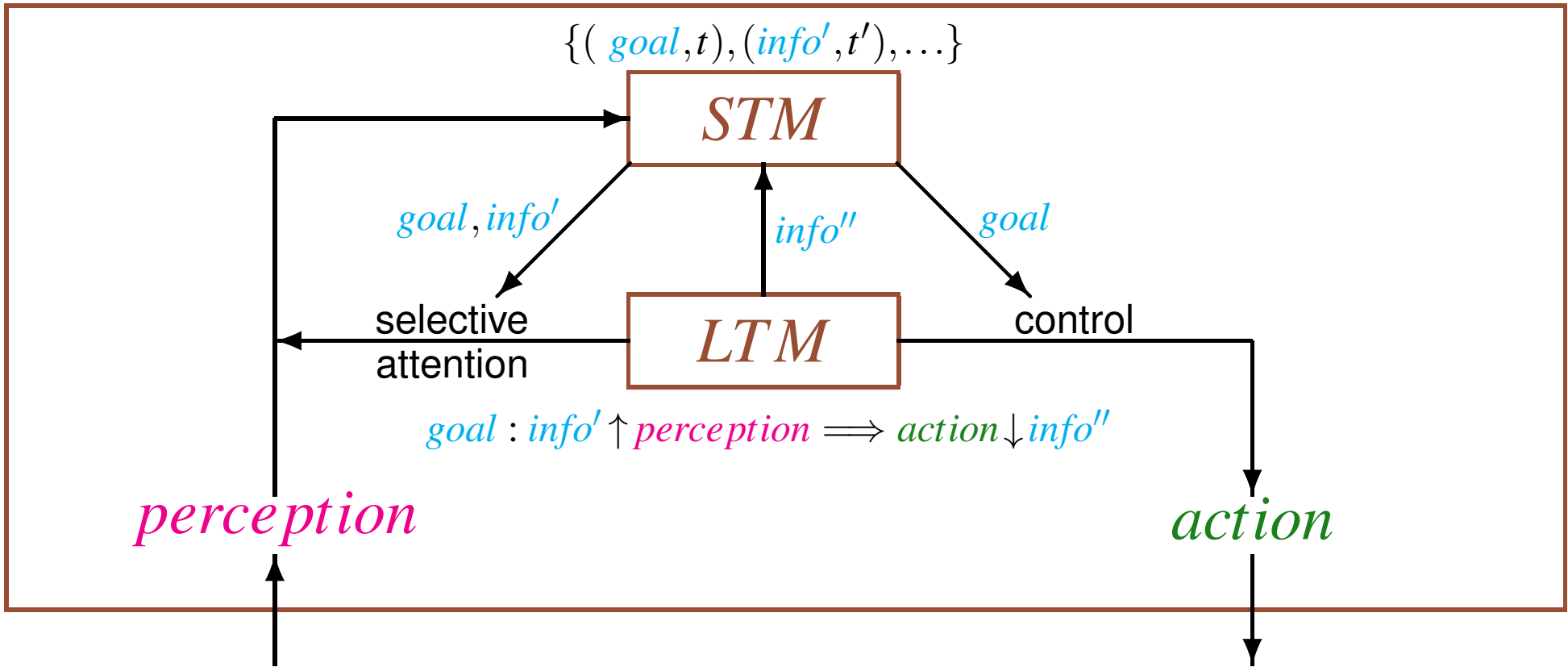


Environment Model

# User Cognitive Model (UCM)

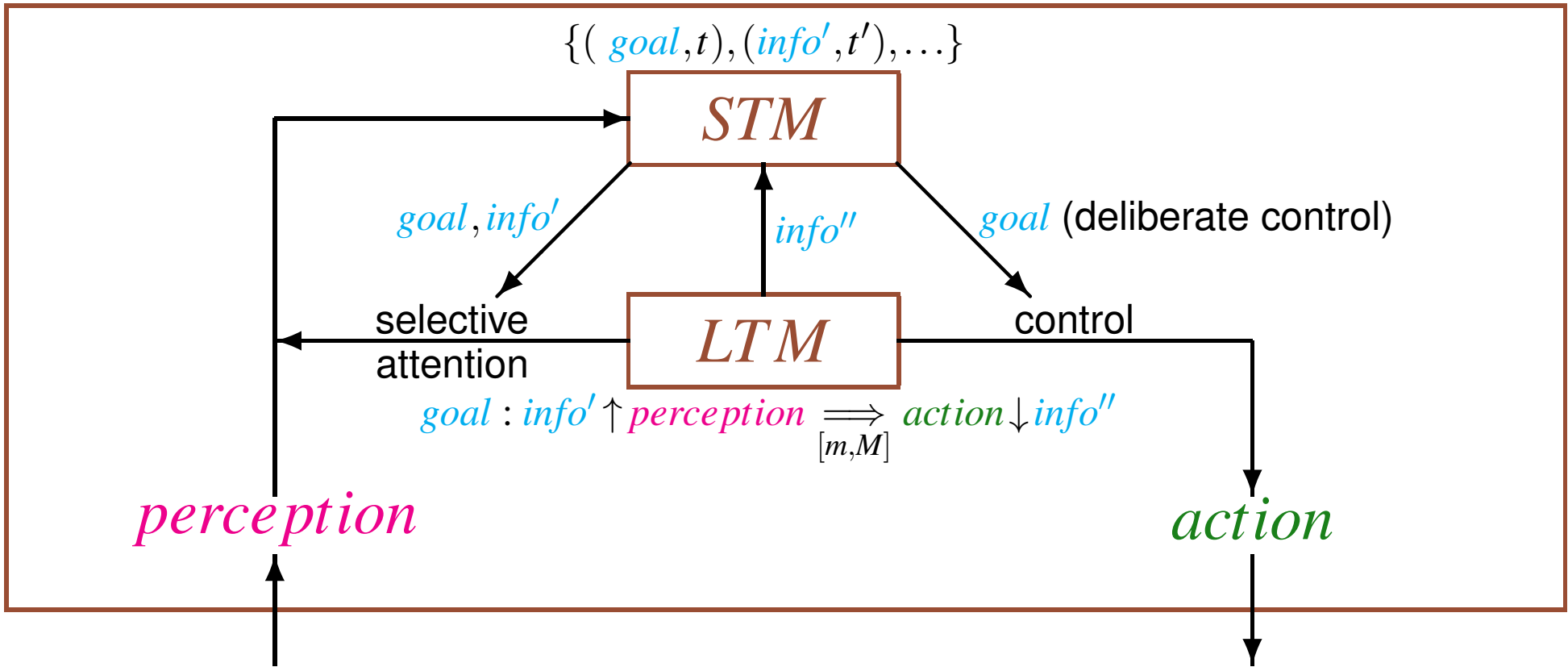


# User Cognitive Model (UCM)



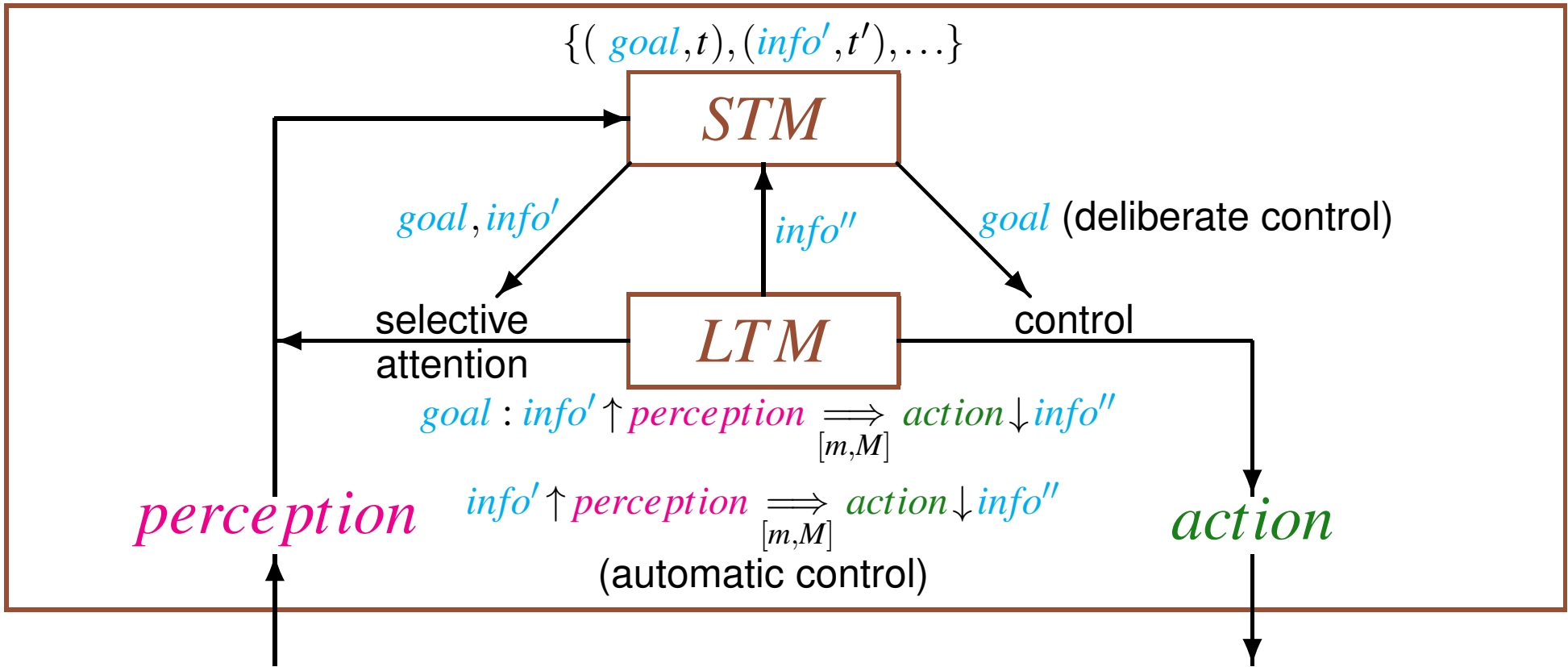
Environment Model

# User Cognitive Model (UCM)



Environment Model

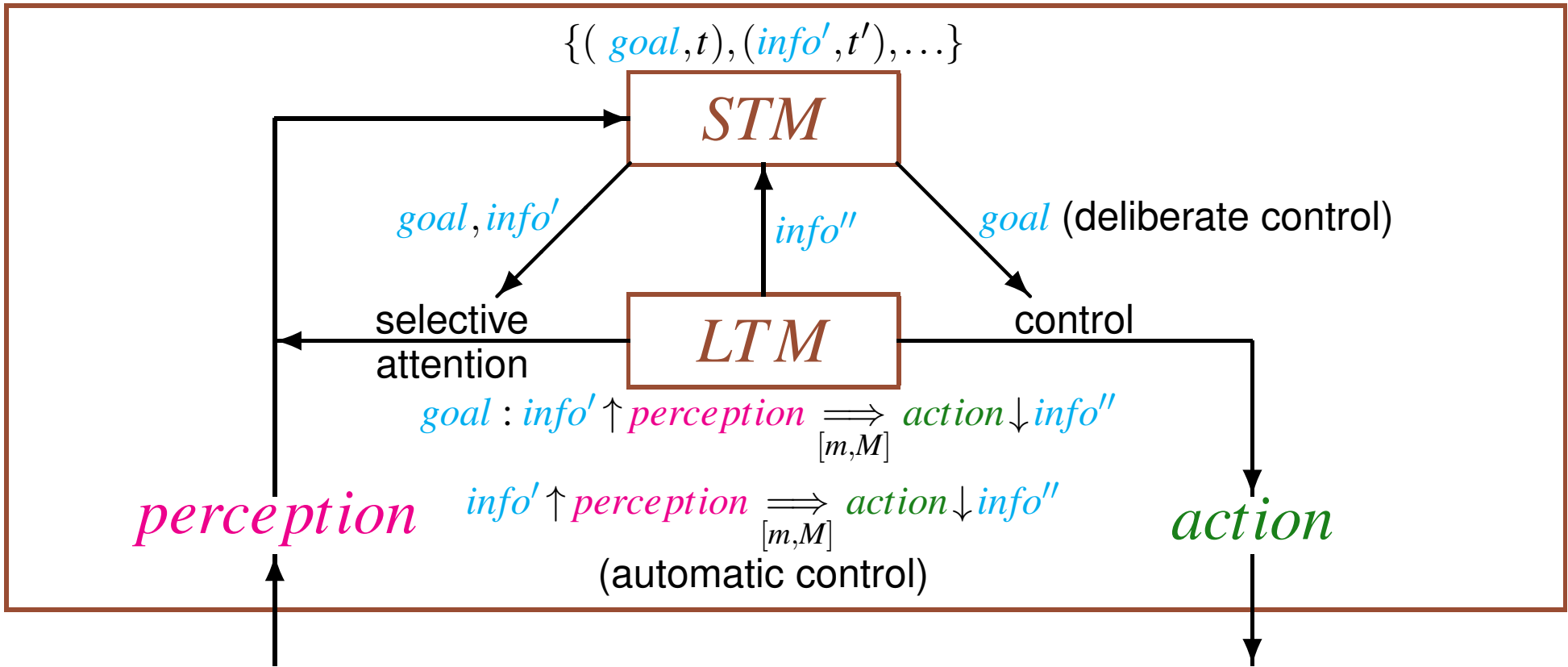
# User Cognitive Model (UCM)



Environment Model

# User Cognitive Model (UCM)

Behaviour and Reasoning Description Language (BRDL)

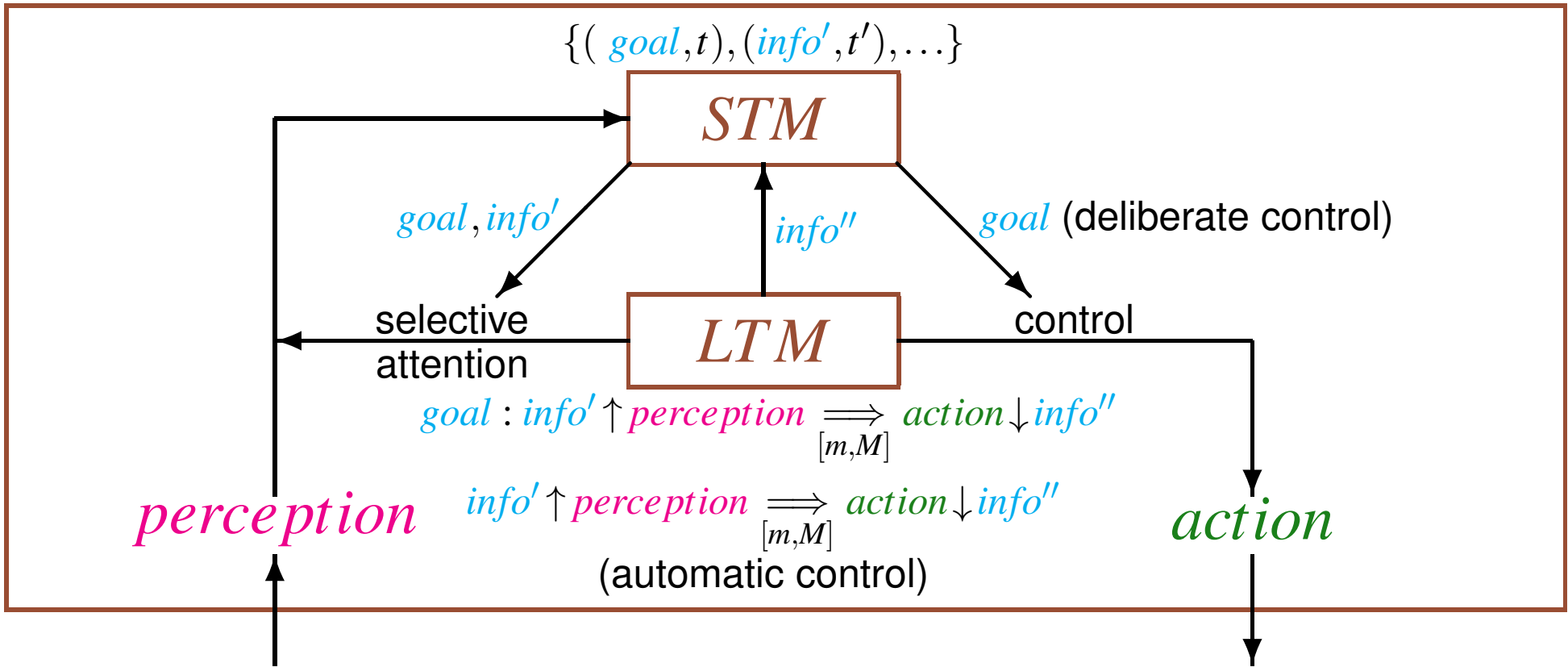


Environment Model



# User Cognitive Model (UCM)

Behaviour and Reasoning Description Language (BRDL)



Environment Model  
(Client Model)

# Example: Student UCM in BRDL

$$\uparrow \text{emptyPage} \xRightarrow{[100,300]} \text{refresh} \downarrow$$

$$\text{goal}(\text{enrolled}) : \uparrow \text{available} \xRightarrow{[100,300]} \text{enrol} \downarrow$$

$$\text{goal}(\text{enrolled}) : \uparrow \text{enrolled} \xRightarrow{[100,300]} \downarrow \text{enrolled}$$

$$\text{goal}(\text{enrolled}) : \text{enrolled} \uparrow \xRightarrow{[100,300]} \text{proceed} \downarrow \text{enrolled}$$

$$\text{goal}(\text{noLab}) : \uparrow \text{chooseLab} \xRightarrow{[100,300]} \text{proceed} \downarrow$$

$$\text{goal}(\text{noLab}) : \uparrow \text{noLab} \xRightarrow{[100,300]} \downarrow \text{noLab}$$

$$\text{goal}(\text{registerLab}) : \uparrow \text{chooseLab} \xRightarrow{[100,300]} \text{registerLab} \downarrow$$

# Client Model

*perception* User Cognitive Model *i*

*action*



Client *i* Model

Communicating Labelled Transition Systems (*CLTS*)

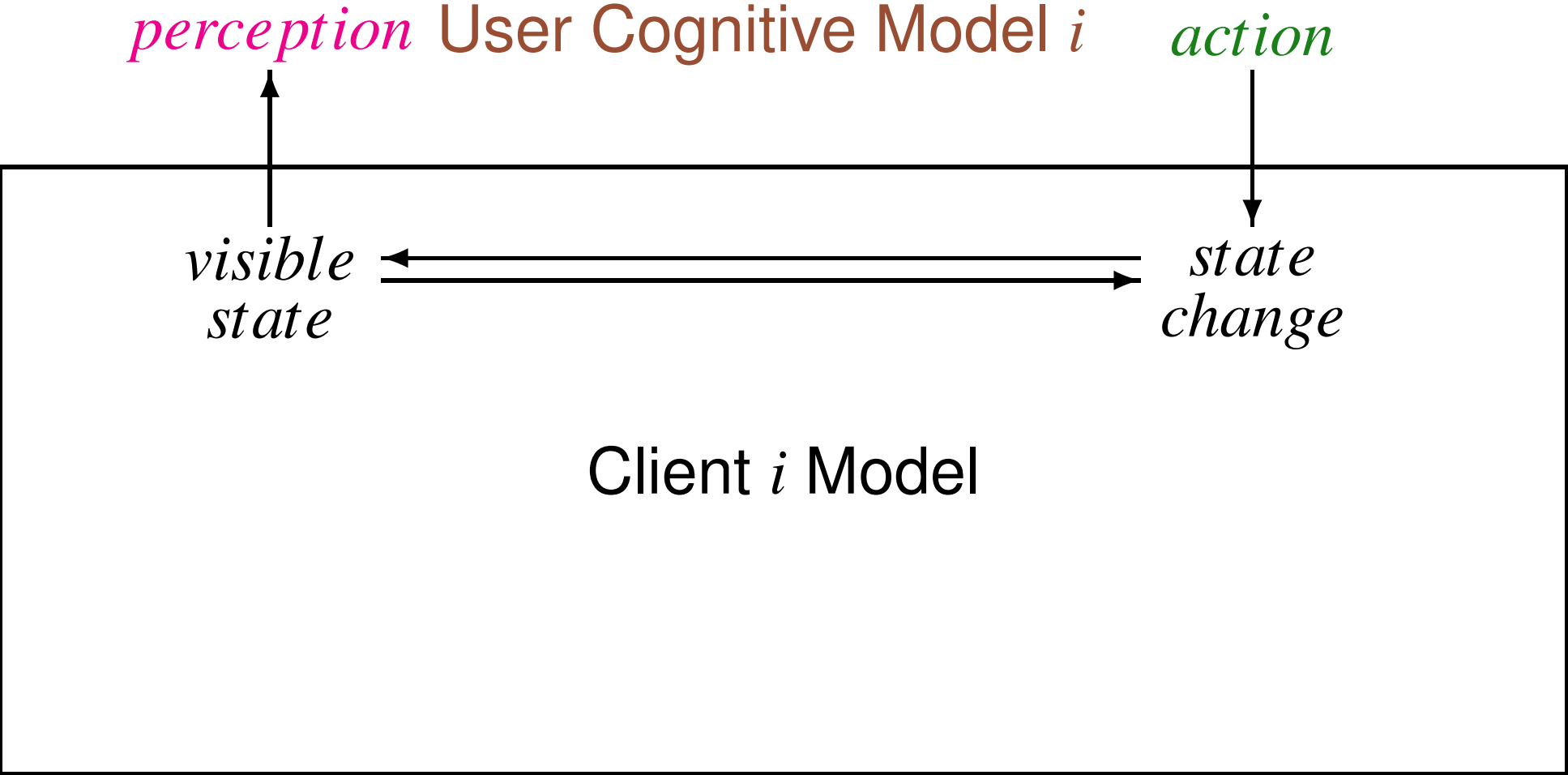
# Client Model

*perception* User Cognitive Model *i* *action*

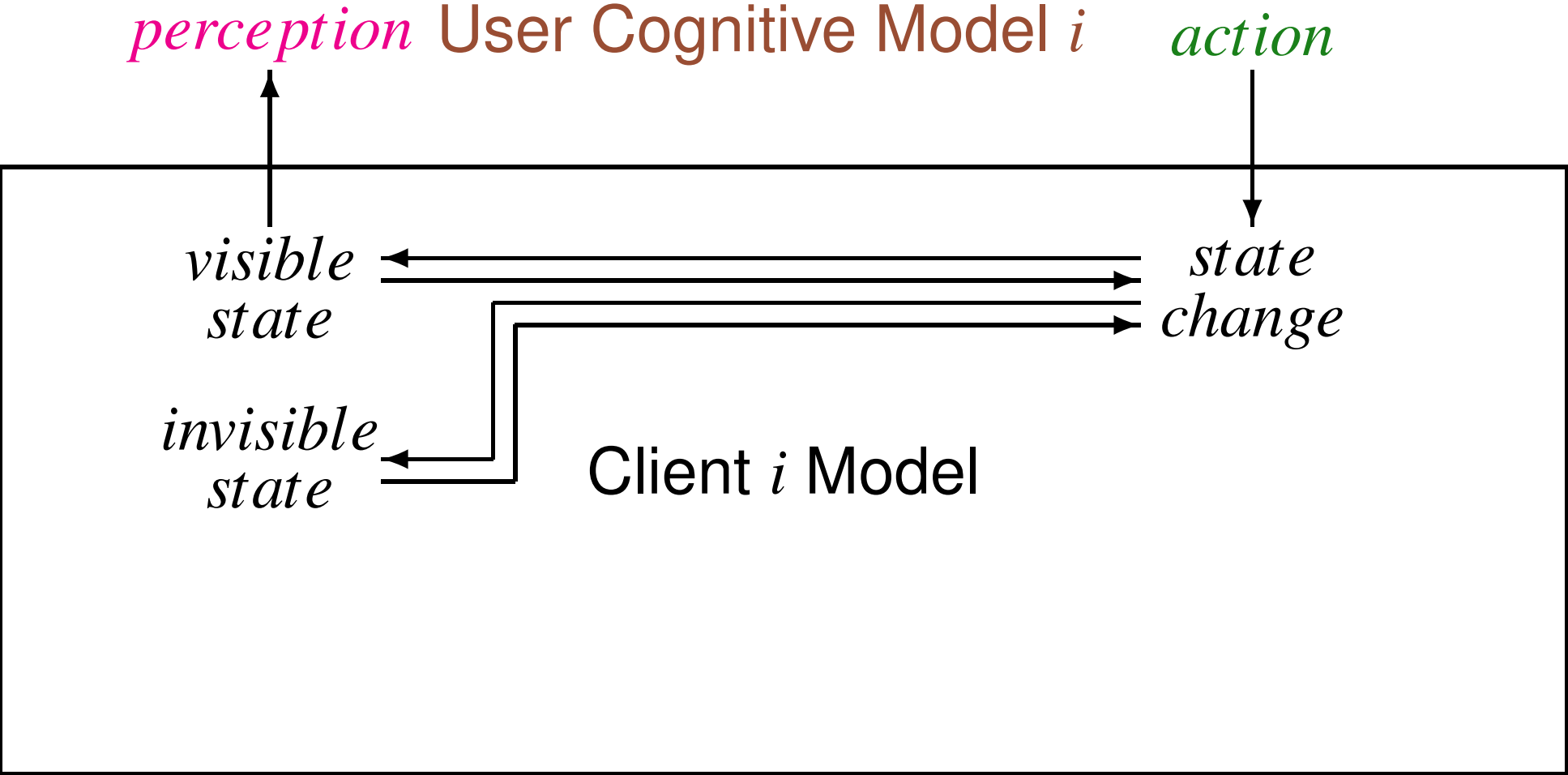
*visible  
state*

Client *i* Model

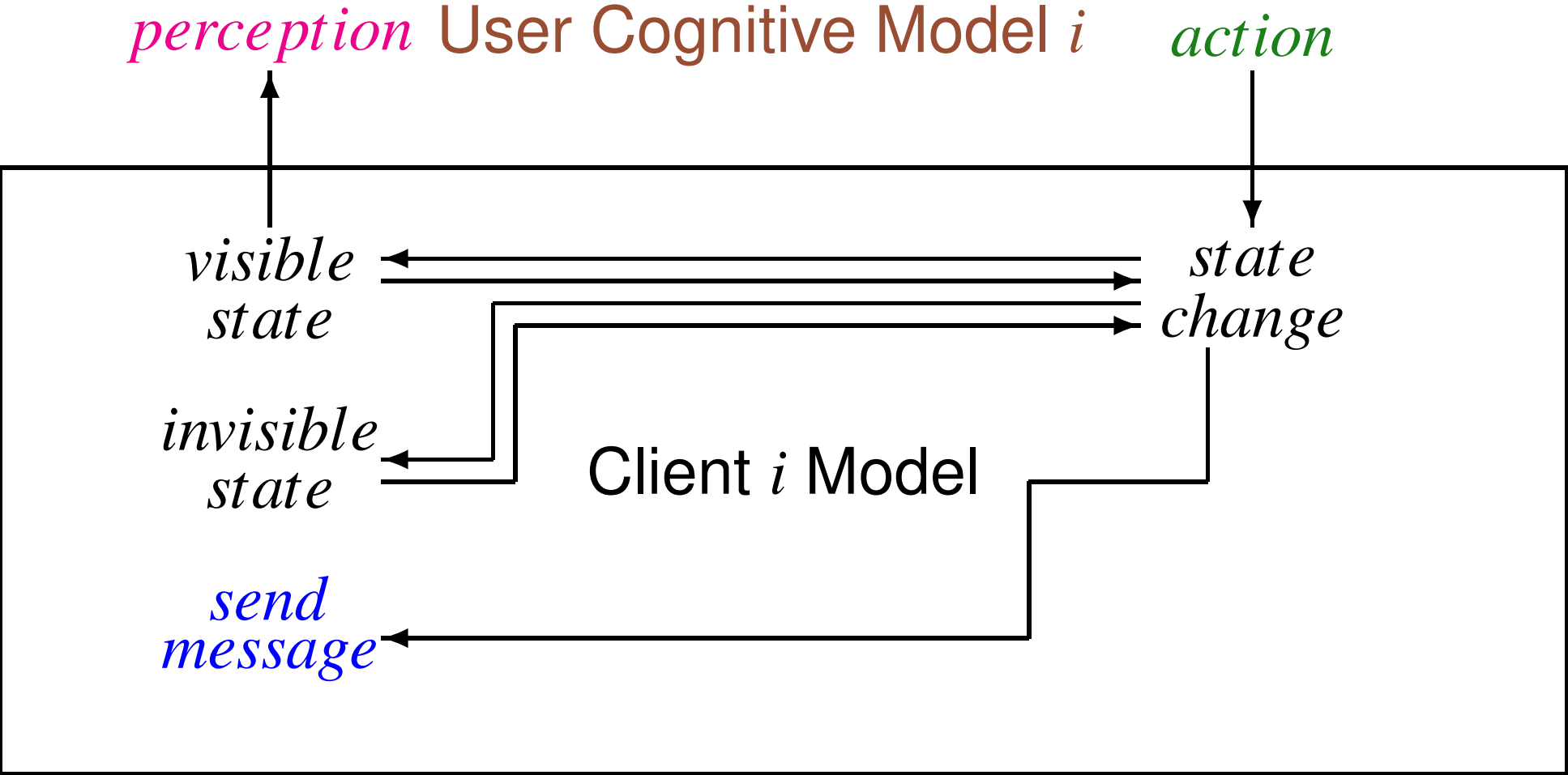
# Client Model



# Client Model

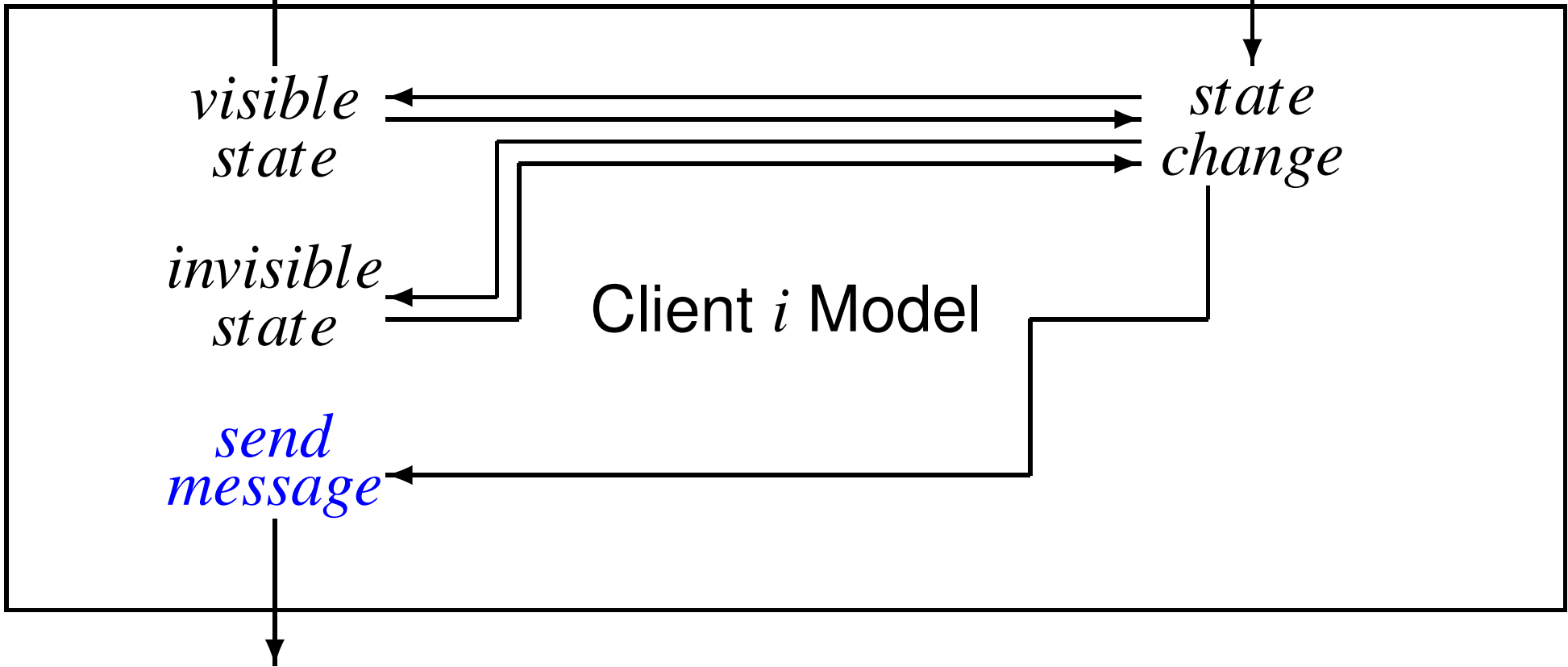


# Client Model



# Client Model

*perception* User Cognitive Model *i* *action*



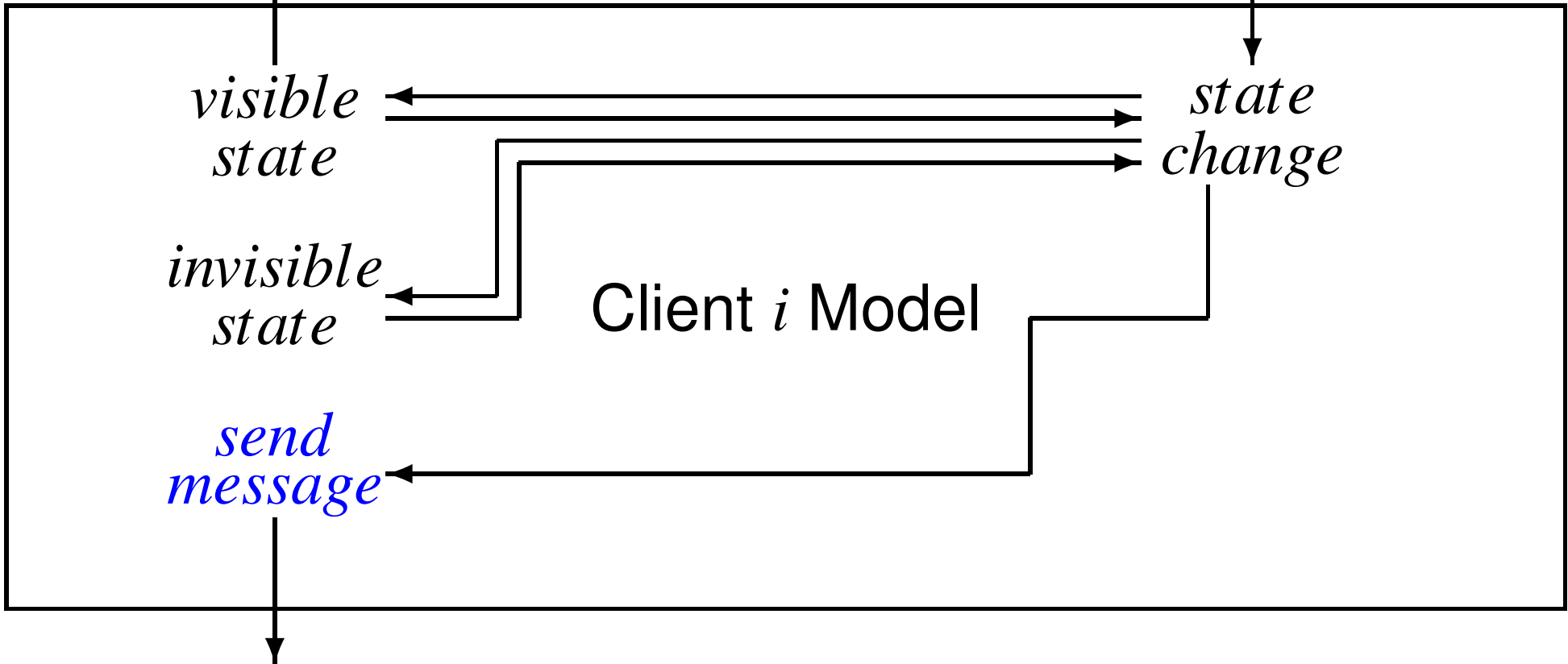
Server Model



# Client Model

*perception* User Cognitive Model *i* *action*

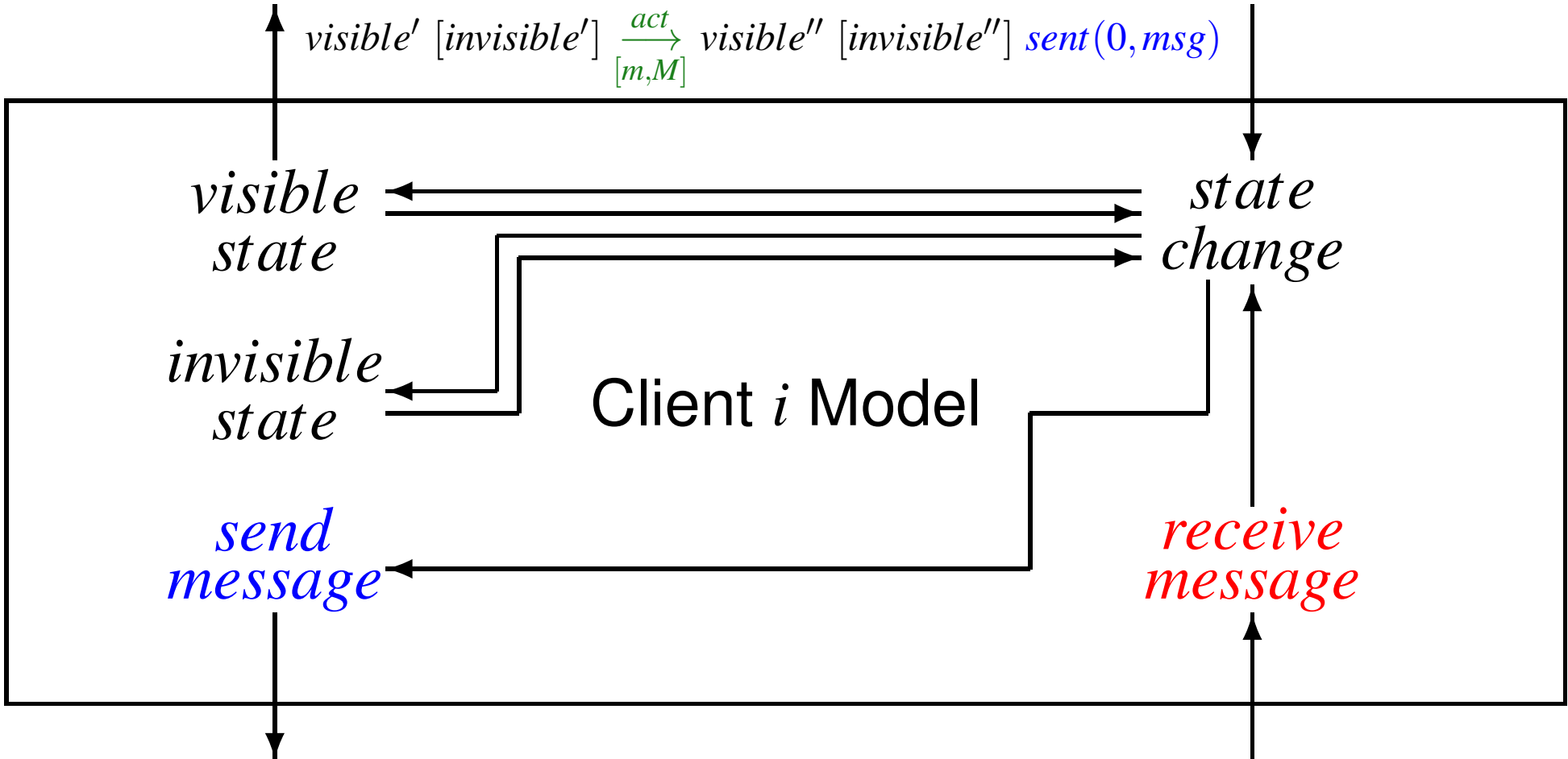
$visible' [invisible'] \xrightarrow[m, M]{act} visible'' [invisible''] sent(0, msg)$



Server Model

# Client Model

*perception* User Cognitive Model *i* *action*

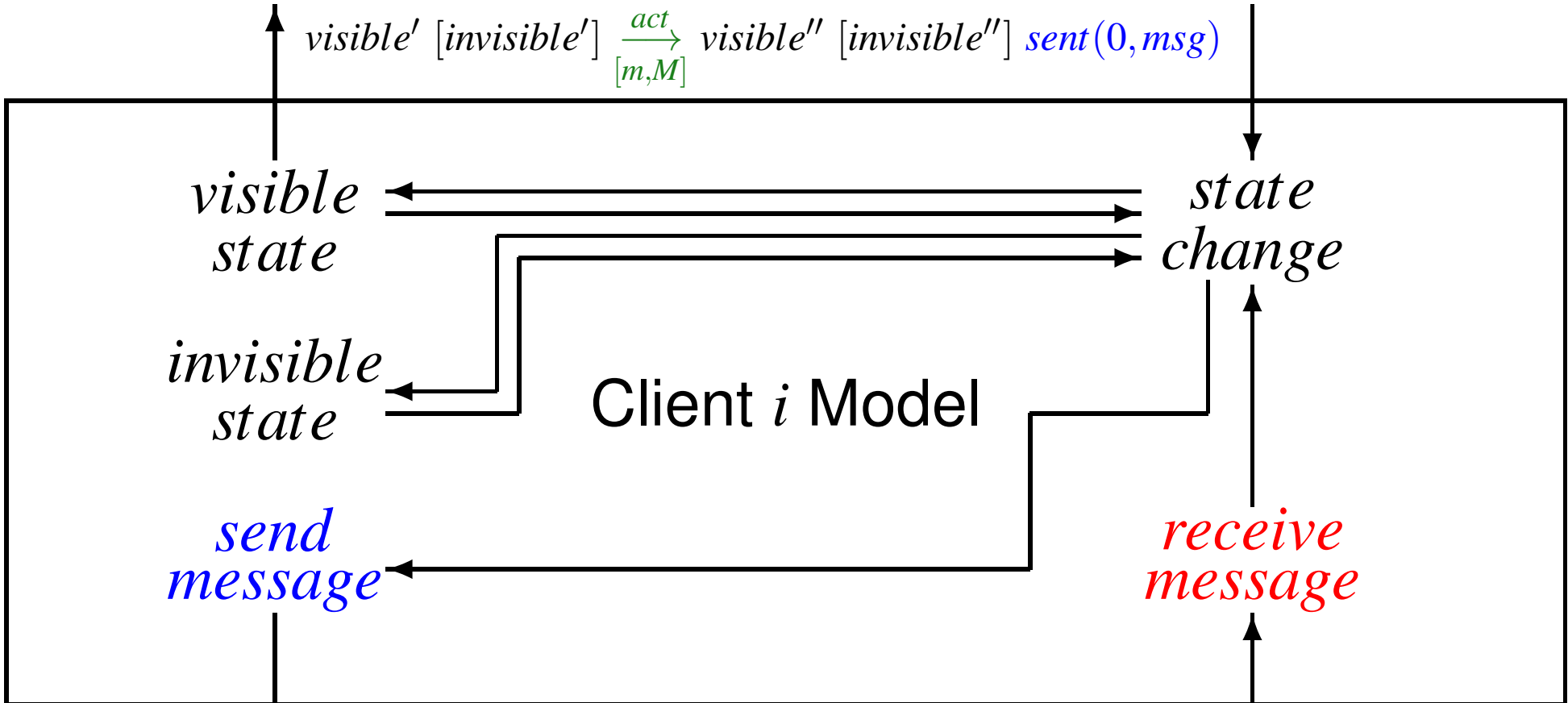


$visible' [invisible'] \xrightarrow[m, M]{act} visible'' [invisible''] sent(0, msg)$

Server Model

# Client Model

*perception* User Cognitive Model *i* *action*



*visible'* [*invisible'*]  $\xrightarrow[\text{[m, M]}]{\text{act}}$  *visible''* [*invisible''*] *sent*(0, *msg*)

*visible'* [*invisible'*]  $\xrightarrow[\text{[m, M]}]{\text{msg}}$  *visible''* [*invisible''*] *sent*(0, *msg*)

Server Model

# Example: Client CLTS

$$\text{emptyPage} [] \xrightarrow[0]{\text{refresh}} \text{waiting} [] \text{ sent}(0, \text{check}_i)$$

$$\text{waiting} [] \xrightarrow[0]{\text{available}} \text{available} []$$

$$\text{waiting} [] \xrightarrow[0]{\text{unavailable}} \text{unavailable} []$$

$$\text{available} [] \xrightarrow[0]{\text{enrol}} \text{enrolled} [\text{labs}] \text{ sent}(0, \text{register}_i)$$

$$\text{enrolled} [\text{labs}] \xrightarrow[0]{\text{proceed}} \text{enrolled} [\text{loadingLabs}] \text{ sent}(0, \text{checkLabs}_i)$$

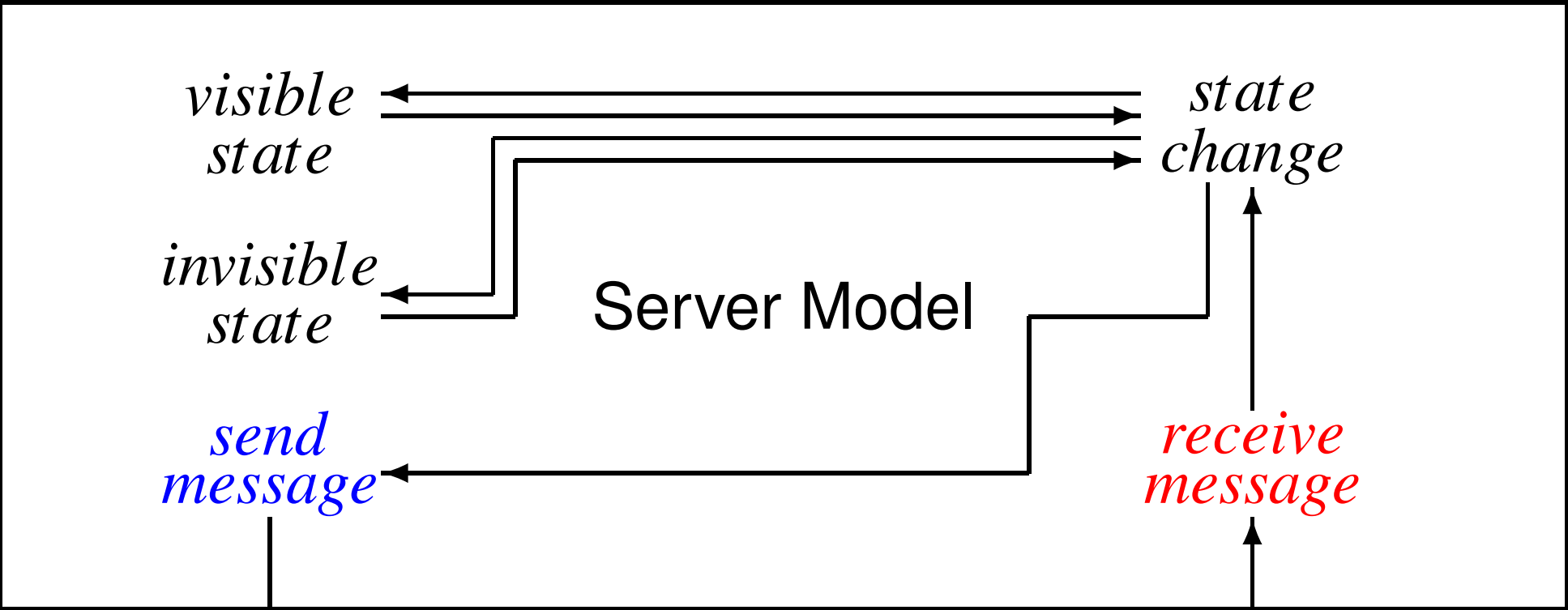
$$\text{enrolled} [\text{loadingLabs}] \xrightarrow[0]{\text{labInfo}} \text{chooseLab} []$$

$$\text{enrolled} [\text{loadingLabs}] \xrightarrow[0]{\text{labFailed}} \text{enrolled} [\text{labs}]$$

$$\text{chooseLab} [] \xrightarrow[0]{\text{proceed}} \text{noLab} []$$

$$\text{chooseLab} [] \xrightarrow[0]{\text{registerLab}} \text{labRegistered} [] \text{ sent}(0, \text{labChosen}_i)$$

# Server Model



$visible' [invisible'] \xrightarrow[m, M]{msg_i} visible'' [invisible''] sent(i, msg)$

## Client *i* Model

# Example: Server CLTS

$$[available] \xrightarrow[10,1000]{check_i} [available] \text{ sent}(i, available)$$

$$[unavailable] \xrightarrow[10,1000]{check_i} [unavailable] \text{ sent}(i, unavailable)$$

$$[available] \xrightarrow[10,1000]{register_i} [unavailable, registered_i]$$

$$[unavailable] \xrightarrow[10,1000]{register_i} [unavailable]$$

$$[] \xrightarrow[10,1000]{checkLabs_i} [] \text{ sent}(i, labInfo)$$

$$[] \xrightarrow[10,1000]{checkLabs_i} [] \text{ sent}(i, labFailed)$$

$$[] \xrightarrow[10,1000]{labChosen_i} [labRegistered_i]$$

# *Overall System Model (OSM)*

Human 1

⋮

Human  $n$

$\{u_j\}_{j \in \mathbb{J}}$

# Overall System Model (OSM)

System  $n + 1$

⋮

System 1

⋮

System  $n$

Human 1

⋮

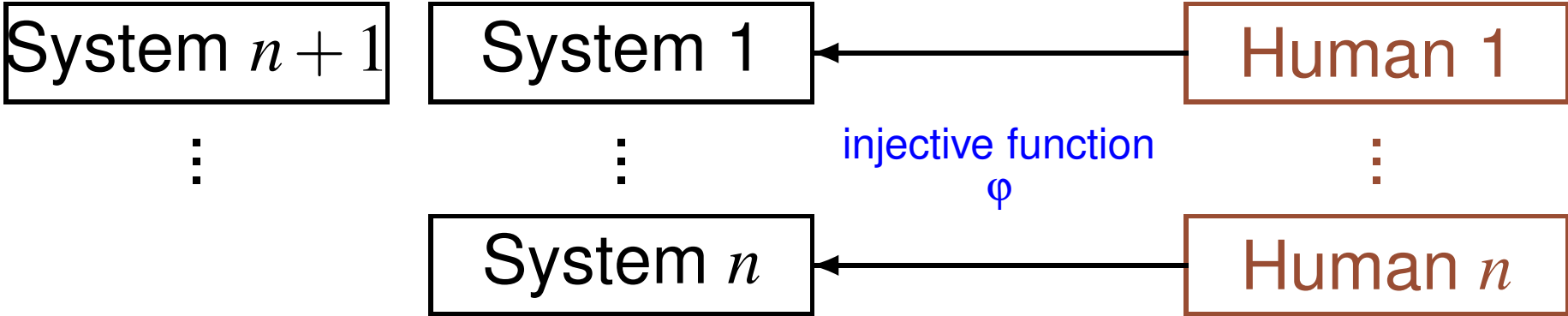
Human  $n$

$\{S_i\}_{i \in \mathbb{I}}$

$\{U_j\}_{j \in \mathbb{J}}$



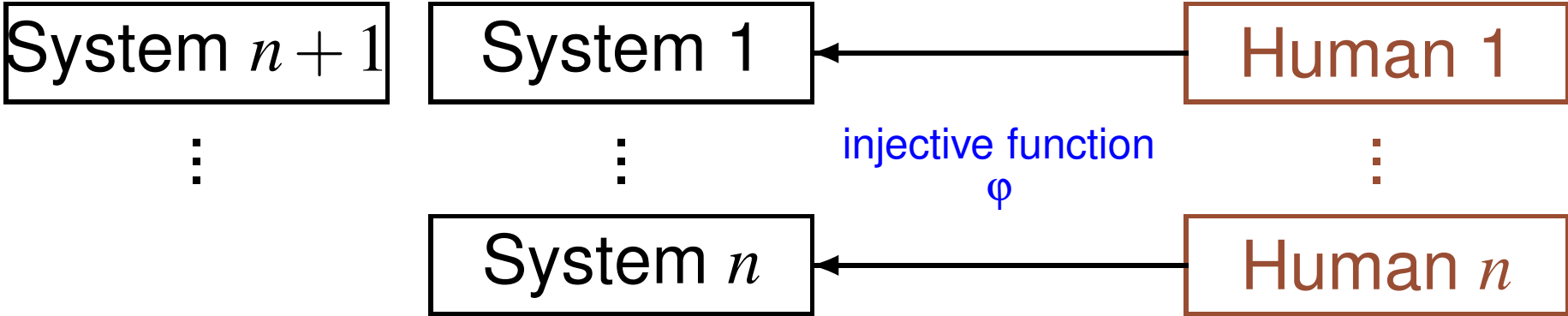
# Overall System Model (OSM)



$$\{S_i\}_{i \in I}$$

$$\{U_j\}_{j \in J}$$

# Overall System Model (OSM)



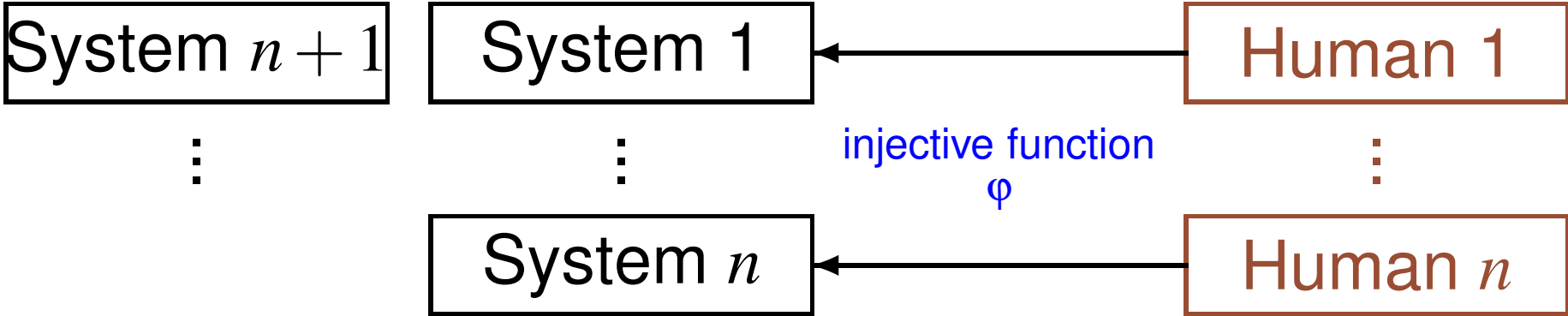
Network

$\{S_i\}_{i \in I}$

$\mu$

$\{U_j\}_{j \in J}$

# Overall System Model (OSM)



Network

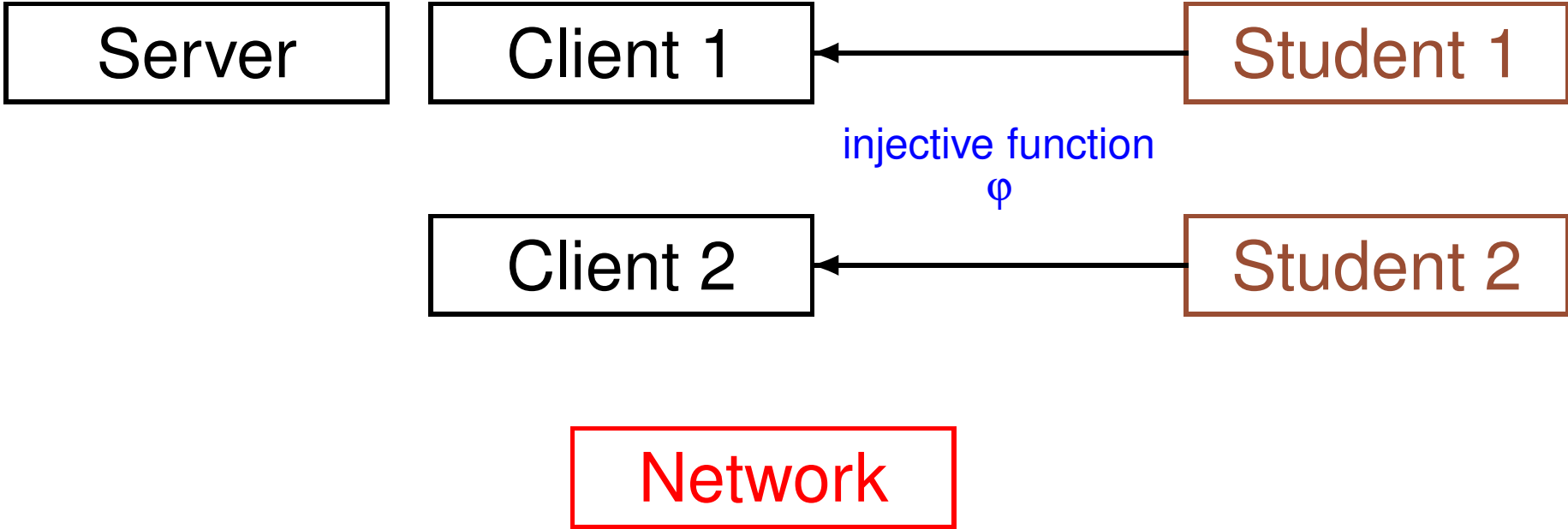
$\{S_i\}_{i \in I}$

$\mu$

$\{U_j\}_{j \in J}$

$$\mathcal{M} = \langle \{S_i\}_{i \in I}, \{U_j\}_{j \in J}, \varphi, \mu \rangle$$

# OSM Example



$\{S_1, S_2\}$

$\emptyset$

$\{U_1, U_2\}$

$$\mathcal{M} = \langle \{S_1, S_2\}, \{U_1, U_2\}, \varphi, \emptyset \rangle$$

# *Cognitive Properties*

1. Only one student believes to have registered for the one place course;
2. A student cannot unintentionally skip the lab registration.

# *Formal Analysis of Cognitive Property 1*

1. Only one student believes to have registered for the one place course.

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**Search Condition:**  $(enrolled, T') \in STM' \wedge (enrolled, T'') \in STM''$

# *Formal Analysis of Cognitive Property 1*

1. Only one student believes to have registered for the one place course.

**Search Condition:**  $(enrolled, T') \in STM' \wedge (enrolled, T'') \in STM''$

The search should fail to validate Property 1



# *Formal Analysis of Cognitive Property 1*

1. Only one student believes to have registered for the one place course.

Search Condition:  $(enrolled, T') \in STM' \wedge (enrolled, T'') \in STM''$

The search should fail to validate Property 1

But it doesn't  $\implies$  **Property 1 does not hold**

# Property 1 Violation: Server Side

1. Only one student believes to have registered for the one place course.

**Search Condition:**  $(enrolled, T') \in STM' \wedge (enrolled, T'') \in STM''$

$$[available] \xrightarrow[10,1000]{check_i} [available] \text{ sent}(i, available)$$

$$[unavailable] \xrightarrow[10,1000]{check_i} [unavailable] \text{ sent}(i, unavailable)$$

$$[available] \xrightarrow[10,1000]{register_i} [unavailable, registered_i]$$

$$[unavailable] \xrightarrow[10,1000]{register_i} [unavailable]$$

$$[] \xrightarrow[10,1000]{checkLabs_i} [] \text{ sent}(i, labInfo)$$

$$[] \xrightarrow[10,1000]{checkLabs_i} [] \text{ sent}(i, labFailed)$$

$$[] \xrightarrow[10,1000]{labChosen_i} [labRegistered_i]$$

# Property 1 Violation: Server Side

1. Only one student believes to have registered for the one place course.

**Search Condition:**  $(enrolled, T') \in STM' \wedge (enrolled, T'') \in STM''$

$$[available] \xrightarrow[10,1000]{check_i} [available] \text{ sent}(i, available)$$

$$[unavailable] \xrightarrow[10,1000]{check_i} [unavailable] \text{ sent}(i, unavailable)$$

$$[available] \xrightarrow[10,1000]{register_i} [unavailable, registered_i]$$

$$[unavailable] \xrightarrow[10,1000]{register_i} [unavailable] \quad (\text{no message is sent to Client } i)$$

$$[] \xrightarrow[10,1000]{checkLabs_i} [] \text{ sent}(i, labInfo)$$

$$[] \xrightarrow[10,1000]{checkLabs_i} [] \text{ sent}(i, labFailed)$$

$$[] \xrightarrow[10,1000]{labChosen_i} [labRegistered_i]$$

# Property 1 Violation: Client Side

$$\text{emptyPage} [] \xrightarrow[0]{\text{refresh}} \text{waiting} [] \text{ sent}(0, \text{check}_i)$$

$$\text{waiting} [] \xrightarrow[0]{\text{available}} \text{available} []$$

$$\text{waiting} [] \xrightarrow[0]{\text{unavailable}} \text{unavailable} []$$

$$\text{available} [] \xrightarrow[0]{\text{enrol}} \text{enrolled} [\text{labs}] \text{ sent}(0, \text{register}_i)$$

$$\text{enrolled} [\text{labs}] \xrightarrow[0]{\text{proceed}} \text{enrolled} [\text{loadingLabs}] \text{ sent}(0, \text{checkLabs}_i)$$

$$\text{enrolled} [\text{loadingLabs}] \xrightarrow[0]{\text{labInfo}} \text{chooseLab} []$$

$$\text{enrolled} [\text{loadingLabs}] \xrightarrow[0]{\text{labFailed}} \text{enrolled} [\text{labs}]$$

$$\text{chooseLab} [] \xrightarrow[0]{\text{proceed}} \text{noLab} []$$

$$\text{chooseLab} [] \xrightarrow[0]{\text{registerLab}} \text{labRegistered} [] \text{ sent}(0, \text{labChosen}_i)$$

# Property 1 Violation: Client Side

$$\text{emptyPage} \xrightarrow[0]{\text{refresh}} \text{waiting} \xrightarrow{\text{sent}(0, \text{check}_i)}$$

$$\text{waiting} \xrightarrow[0]{\text{available}} \text{available}$$

$$\text{waiting} \xrightarrow[0]{\text{unavailable}} \text{unavailable}$$

$$\text{available} \xrightarrow[0]{\text{enrol}} \text{enrolled} [\text{labs}] \xrightarrow{\text{sent}(0, \text{register}_i)} \quad (\text{immediate feedback to the user})$$

$$\text{enrolled} [\text{labs}] \xrightarrow[0]{\text{proceed}} \text{enrolled} [\text{loadingLabs}] \xrightarrow{\text{sent}(0, \text{checkLabs}_i)}$$

$$\text{enrolled} [\text{loadingLabs}] \xrightarrow[0]{\text{labInfo}} \text{chooseLab}$$

$$\text{enrolled} [\text{loadingLabs}] \xrightarrow[0]{\text{labFailed}} \text{enrolled} [\text{labs}]$$

$$\text{chooseLab} \xrightarrow[0]{\text{proceed}} \text{noLab}$$

$$\text{chooseLab} \xrightarrow[0]{\text{registerLab}} \text{labRegistered} \xrightarrow{\text{sent}(0, \text{labChosen}_i)}$$

# *Formal Analysis of Cognitive Property 2*

2. A student cannot unintentionally skip the lab registration.

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2. A student cannot unintentionally skip the lab registration.

**Search Condition:** there is a Client which may reach  
a visible state that contains *noLab*  
when starting with  $goal(registerLab) \in STM$

# *Formal Analysis of Cognitive Property 2*

2. A student cannot unintentionally skip the lab registration.

**Search Condition:** there is a Client which may reach  
a visible state that contains *noLab*  
when starting with  $goal(registerLab) \in STM$

The search should fail to validate Property 2



# Formal Analysis of Cognitive Property 2

2. A student cannot unintentionally skip the lab registration.

**Search Condition:** there is a Client which may reach  
a visible state that contains *noLab*  
when starting with  $goal(registerLab) \in STM$

## The search should fail to validate Property 2

(The search should instead succeed when starting with  $goal(noLab) \in STM$ )

# Formal Analysis of Cognitive Property 2

2. A student cannot unintentionally skip the lab registration.

**Search Condition:** there is a Client which may reach  
a visible state that contains *noLab*  
when starting with  $goal(registerLab) \in STM$

The search should fail to validate Property 2

(The search should instead succeed when starting with  $goal(noLab) \in STM$ )

But it doesn't  $\implies$  **Property 2 does not hold**

# Property 2 Violation: Client Side

$$\text{emptyPage} [] \xrightarrow[0]{\text{refresh}} \text{waiting} [] \text{ sent}(0, \text{check}_i)$$

$$\text{waiting} [] \xrightarrow[0]{\text{available}} \text{available} []$$

$$\text{waiting} [] \xrightarrow[0]{\text{unavailable}} \text{unavailable} []$$

$$\text{available} [] \xrightarrow[0]{\text{enrol}} \text{enrolled} [\text{labs}] \text{ sent}(0, \text{register}_i)$$

$$\text{enrolled} [\text{labs}] \xrightarrow[0]{\text{proceed}} \text{enrolled} [\text{loadingLabs}] \text{ sent}(0, \text{checkLabs}_i)$$

$$\text{enrolled} [\text{loadingLabs}] \xrightarrow[0]{\text{labInfo}} \text{chooseLab} []$$

$$\text{enrolled} [\text{loadingLabs}] \xrightarrow[0]{\text{labFailed}} \text{enrolled} [\text{labs}]$$

$$\text{chooseLab} [] \xrightarrow[0]{\text{proceed}} \text{noLab} []$$

# Property 2 Violation: Client Side

$$\text{emptyPage} [] \xrightarrow[0]{\text{refresh}} \text{waiting} [] \text{ sent}(0, \text{check}_i)$$

$$\text{waiting} [] \xrightarrow[0]{\text{available}} \text{available} []$$

$$\text{waiting} [] \xrightarrow[0]{\text{unavailable}} \text{unavailable} []$$

$$\text{available} [] \xrightarrow[0]{\text{enrol}} \text{enrolled} [\text{labs}] \text{ sent}(0, \text{register}_i)$$

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$$\text{enrolled} [\text{loadingLabs}] \xrightarrow[0]{\text{labFailed}} \text{enrolled} [\text{labs}]$$

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$$\text{enrolled} [\text{loadingLabs}] \xrightarrow[0]{\text{labInfo}} \text{chooseLab} []$$

$$\text{enrolled} [\text{loadingLabs}] \xrightarrow[0]{\text{labFailed}} \text{enrolled} [\text{labs}]$$

$$\text{chooseLab} [] \xrightarrow[0]{\text{proceed}} \text{noLab} []$$

the user  
keeps clicking *proceed*  
to register for a lab

# Property 2 Violation: Client Side

$$\text{emptyPage} [] \xrightarrow[0]{\text{refresh}} \text{waiting} [] \text{ sent}(0, \text{check}_i)$$

$$\text{waiting} [] \xrightarrow[0]{\text{available}} \text{available} []$$

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$$\text{enrolled} [\text{loadingLabs}] \xrightarrow[0]{\text{labInfo}} \text{chooseLab} []$$

$$\text{enrolled} [\text{loadingLabs}] \xrightarrow[0]{\text{labFailed}} \text{enrolled} [\text{labs}]$$

$$\text{chooseLab} [] \xrightarrow[0]{\text{proceed}} \text{noLab} []$$

the user  
keeps clicking *proceed*  
to register for a lab

BUT

skips the lab registration instead

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- we are exploring ways to **dynamically assign** users to interfaces

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